

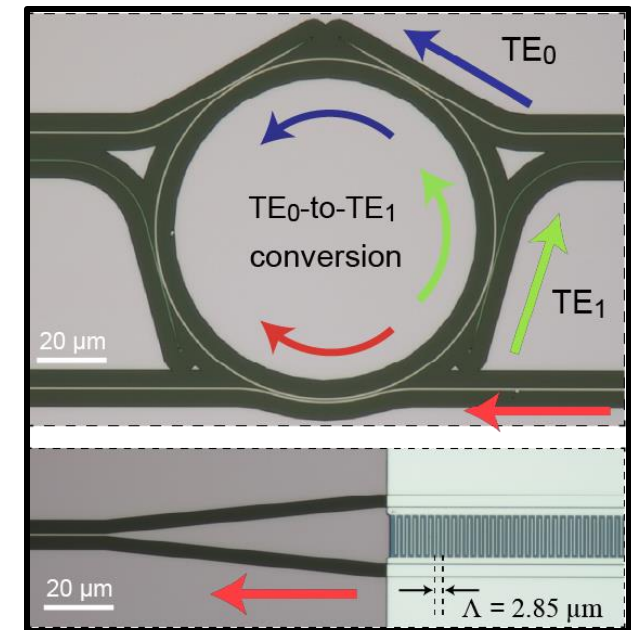
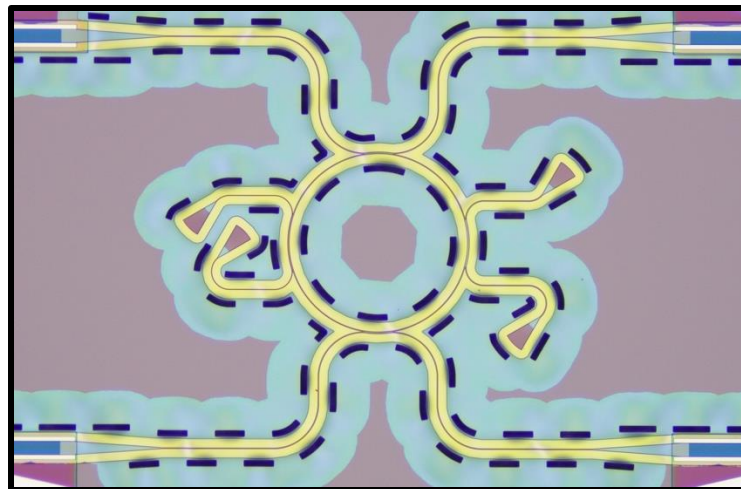
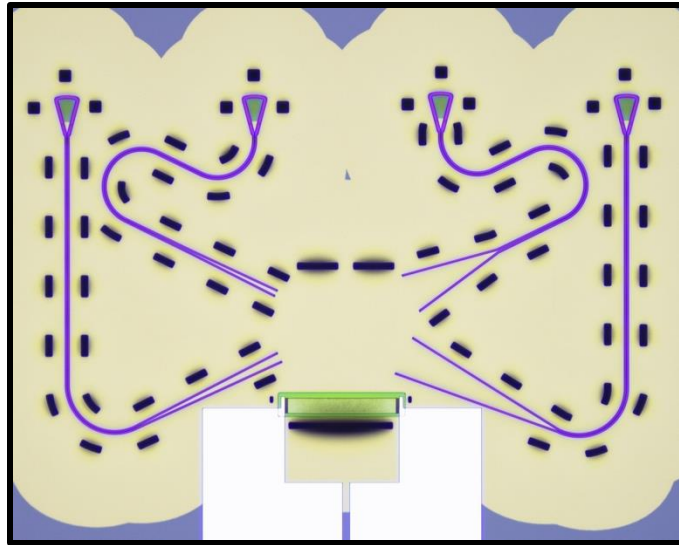
Optomechanical Integrated Circuits for Efficient Microwave-to-Optical Transduction

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University of Washington, Seattle, WA



Motivation for microwave-to-optical transduction

November 2024, IBM Quantum



December 2024, Google Quantum AI

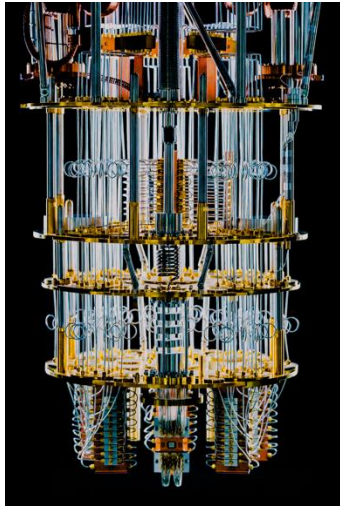


Systems	N_{qubits}	$F_{single-qb}$	F_{two-qb}
IBM Quantum	156		
Google quantum AI	105		~99.96%
		↓ Enormous gap!	
Practical quantum advantage* (M. Beverland et al, 2022)	$>10^6$		$> 99.999\%$

*Depending on the type of error correction scheme used but more or less in this range

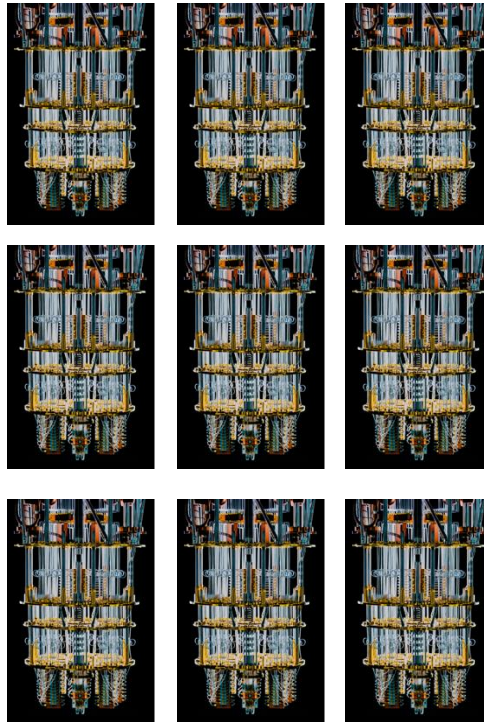
Optical interconnection for qubits

Many qubits in
one fridge
(a thousand)

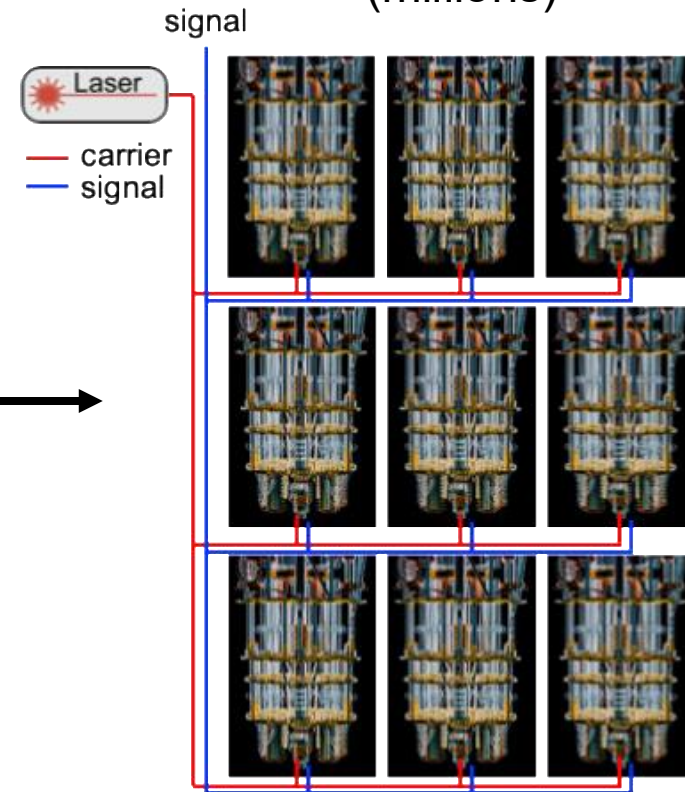


IBM Quantum computer at Yorktown Heights,
Nov. 8, 2021. (PHOTOGRAPH BY BENEDICT EVANS)

Many qubits in
many fridges
(ten thousands)



Optical
interconnected qubits
(millions)



Limitations:
Coaxial cables^[1]
Cooling powers^[2]

Not enough

Optical fibers:
Dilfridge's cooling power at MXC~
one million fibers' passive heat load^[3]

This requires microwave-to-optical transduction!

[1] Kim, Y. et al. Nature 618, 500–505 (2023)

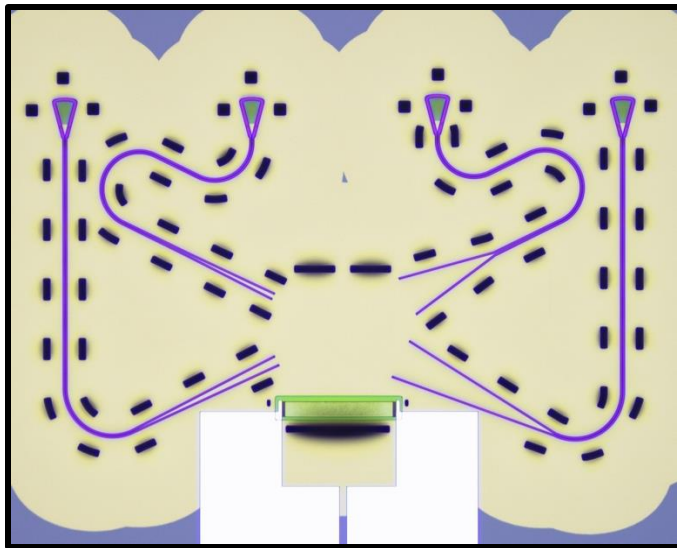
[2] S. Joshi and S. Moazeni, J. of Lightwave Technology, vol. 42, no. 1, pp. 166-175, (2024)

[3] Lecocq, F., et al. Nature 591, 575–579 (2021).

Overview

- **Introduction and examples of microwave-to-optical transductions**
 - **Traveling waves:** acousto-optics through phase-matching condition
 - **Standing waves:** cavity-optomechanics through moving boundary and photoelastic effects
- **Optomechanical integrated circuits (OMIC)** for microwave-to-optical transduction

Acousto-optics frequency shifter (AOFS)

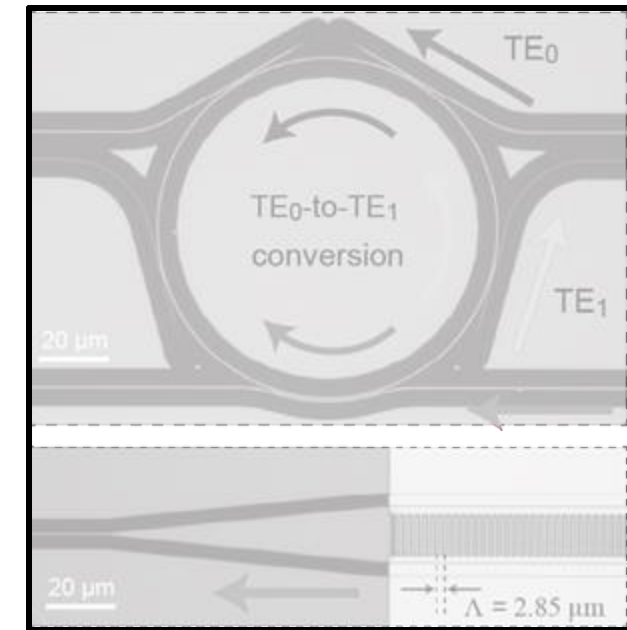


N. S. Yama*, I.-T. Chen* et al., *Advanced Materials* (2023)

Microwave-to-optical transduction



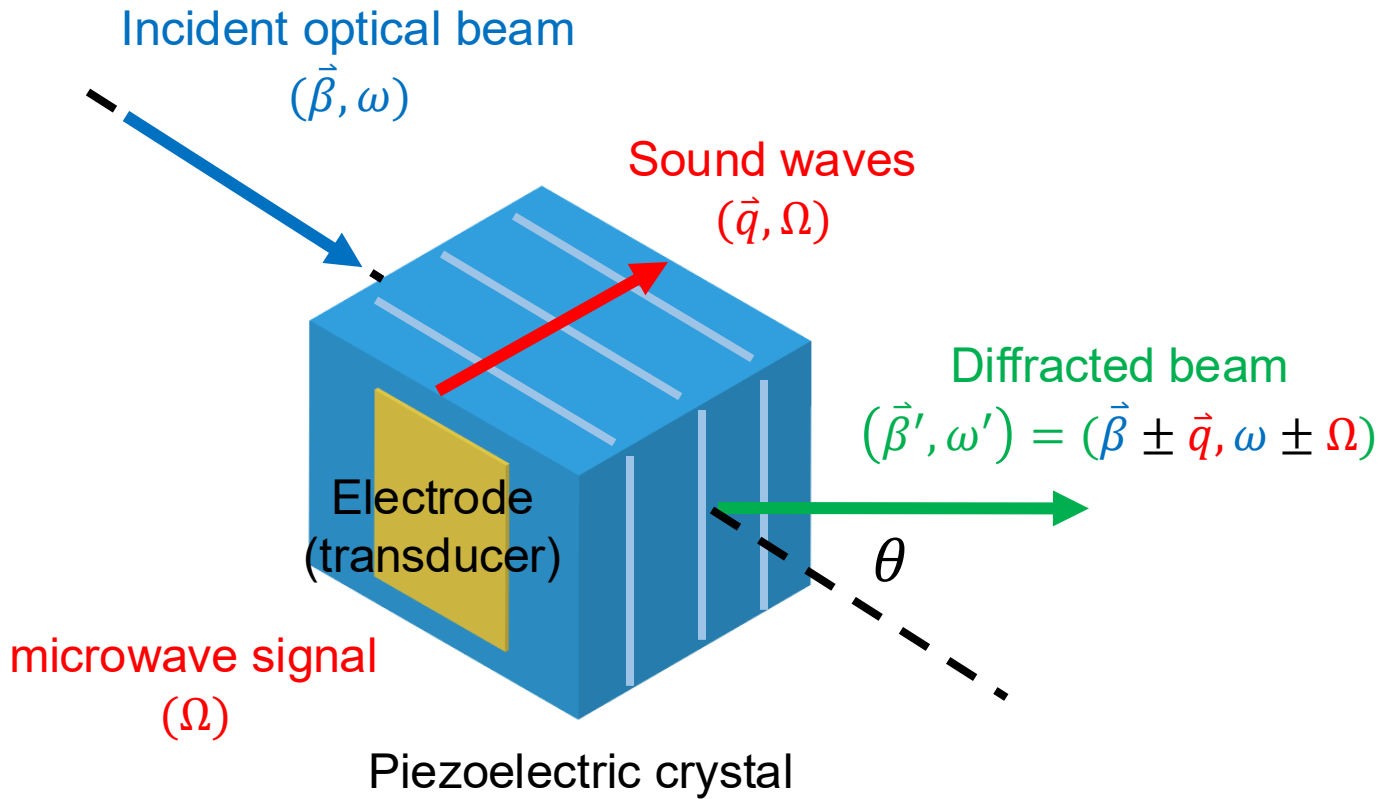
I.-T. Chen et al., *Nat. Commun* (2023)



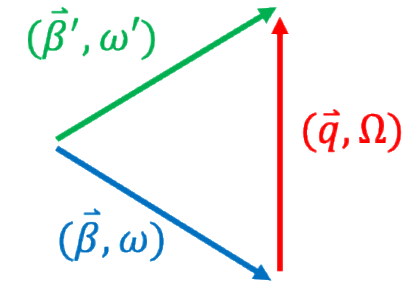
I.-T. Chen et al., *submitted* (2025)

Introduction to microwave-to-optical transduction

One of the simplest ways to convert microwave signal to optical frequency (classical)



Brillouin scattering, which satisfy the phase-matching condition



$$(\vec{\beta}', \omega') = (\vec{\beta} \pm \vec{q}, \omega \pm \Omega)$$

(+): Anti-Stokes: absorbs phonon

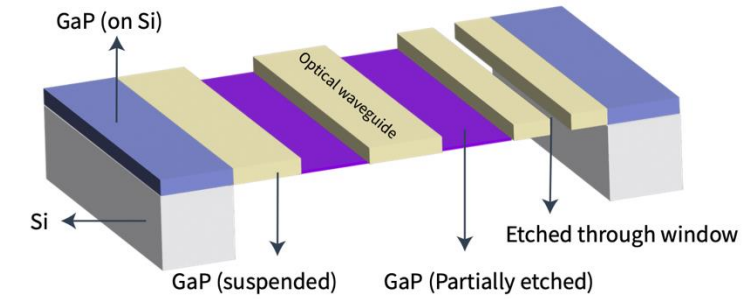
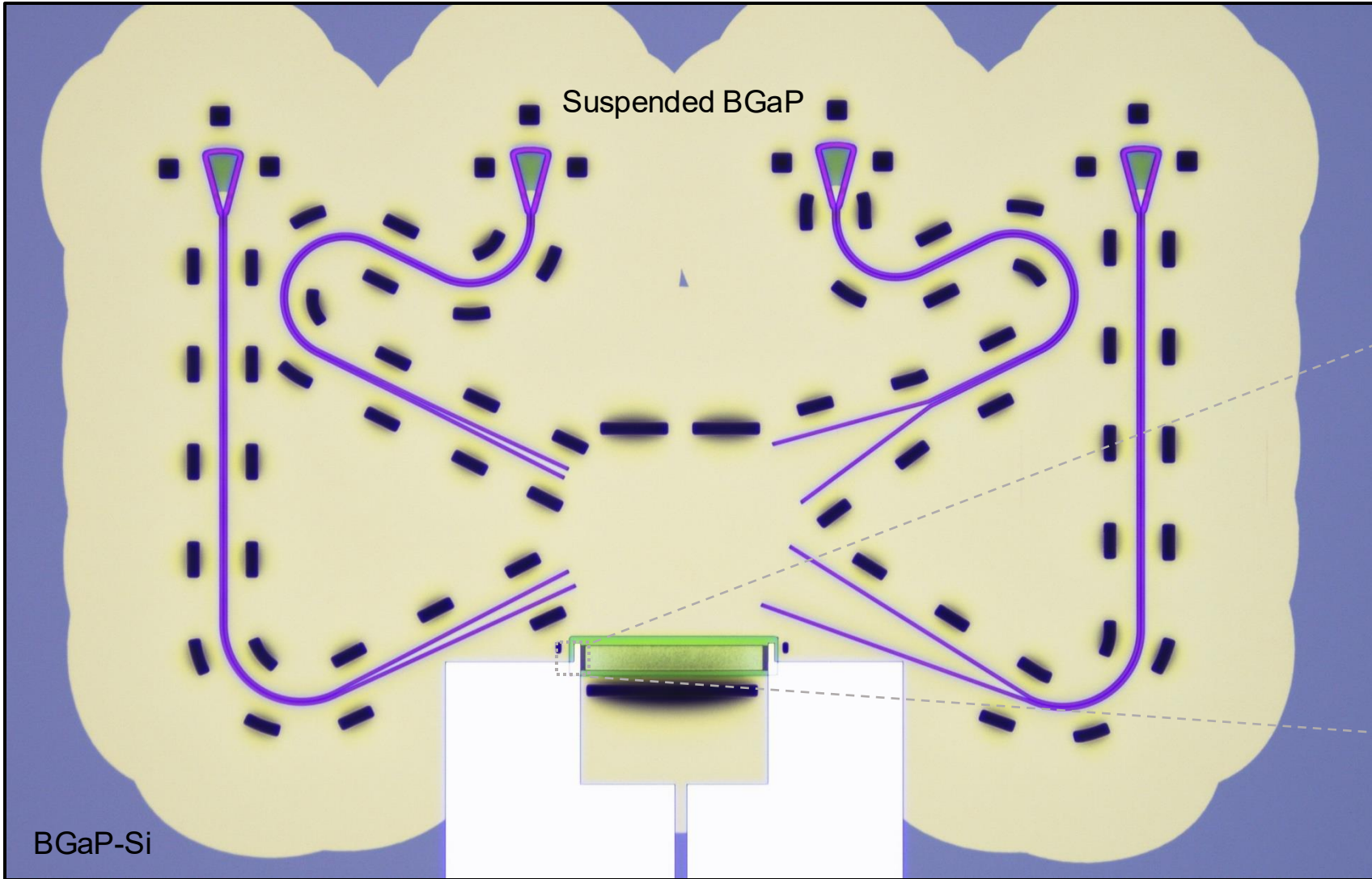
(-): Stokes: emits phonon

Microwave → Sound (phonons) → Optical signal

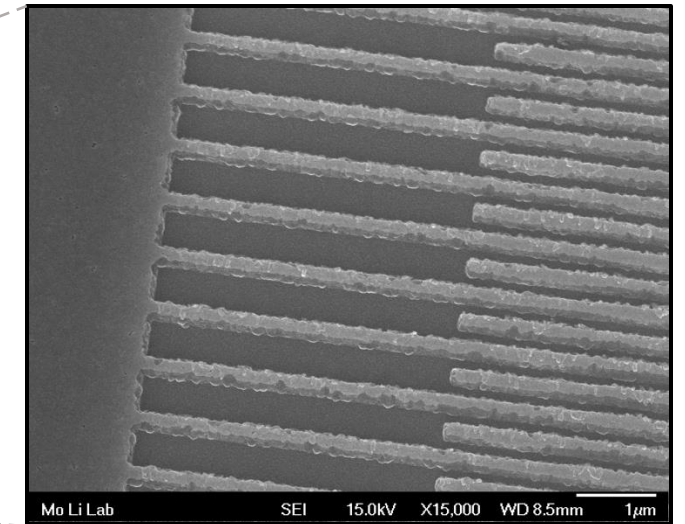
Other methods: electro-optics^[1]. Here, we choose phonon because of its high conversion efficiency and scalability

Brillouin scattering: an example

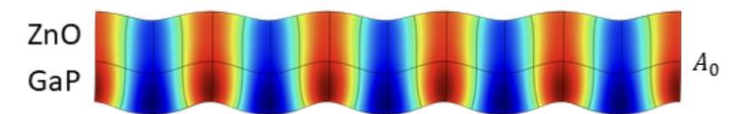
Boron-doped Gallium Phosphide (BGaP): Acousto-Optics Frequency Shifter



IDT on ZnO to excite acoustic waves

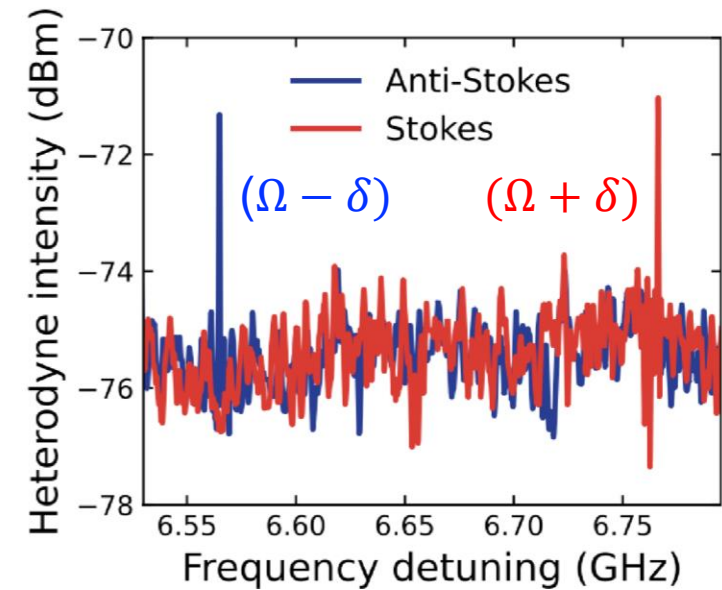
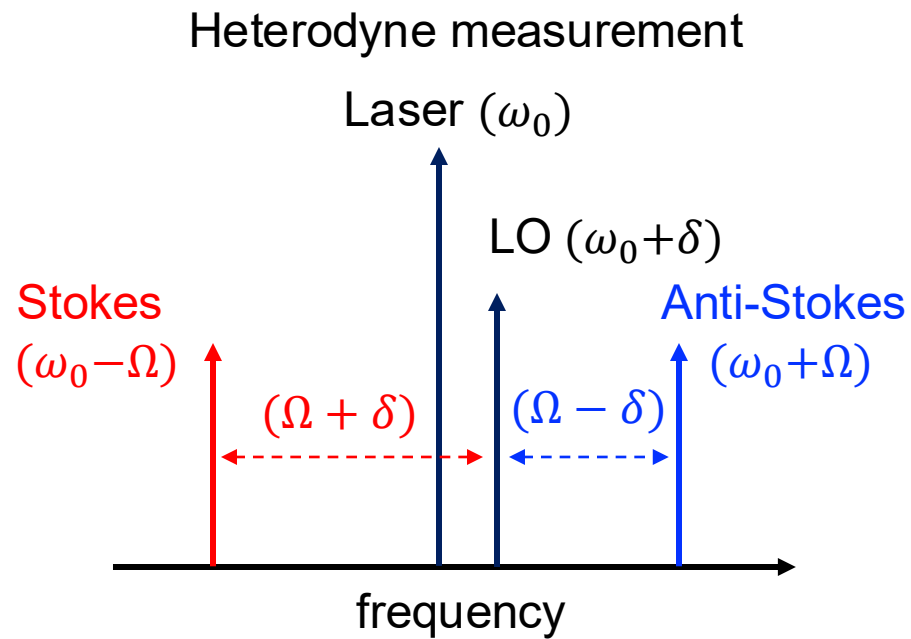
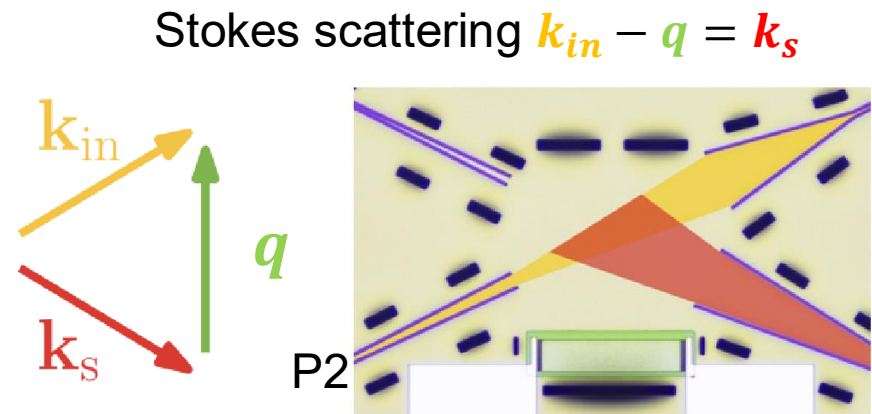
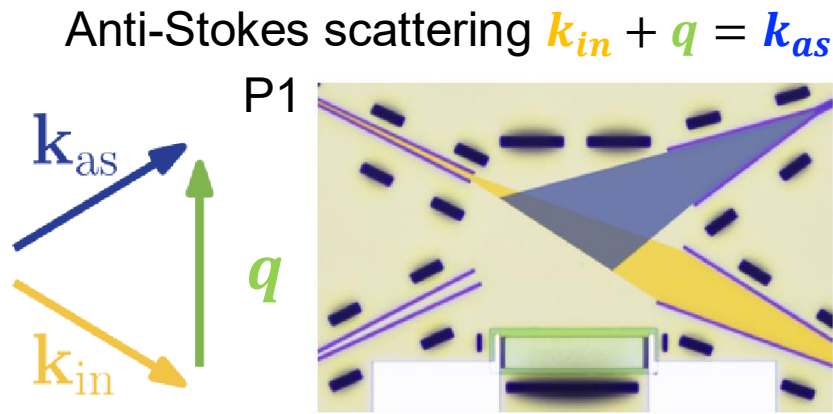
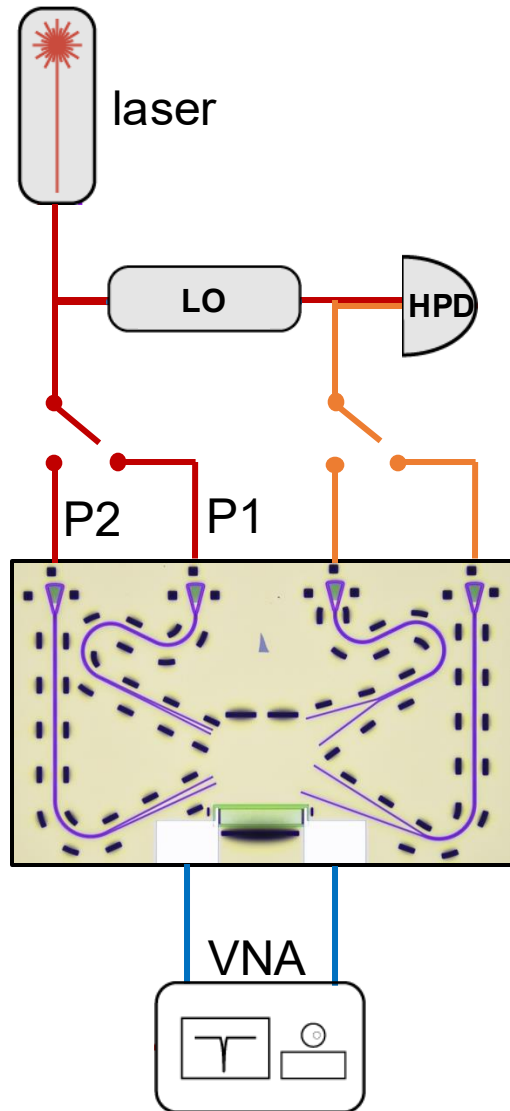


BGaP: weakly piezoelectric



Acoustic wave profile

Brillouin scattering: heterodyne measurement technique

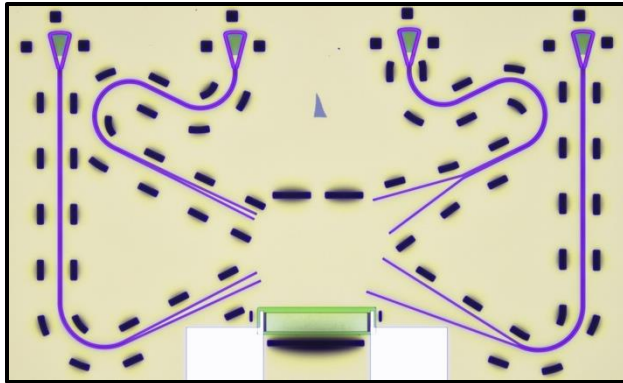


Microwave → Sound (phonons) → Optical signal

How to enhance the photon-phonon interaction?

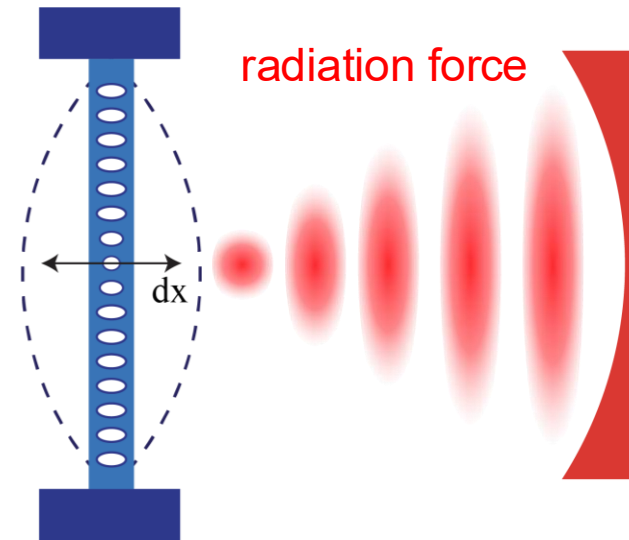
Microwave → **Sound (phonons)** → **Optical signal (photons)**

Traveling waves:
phase-matching condition



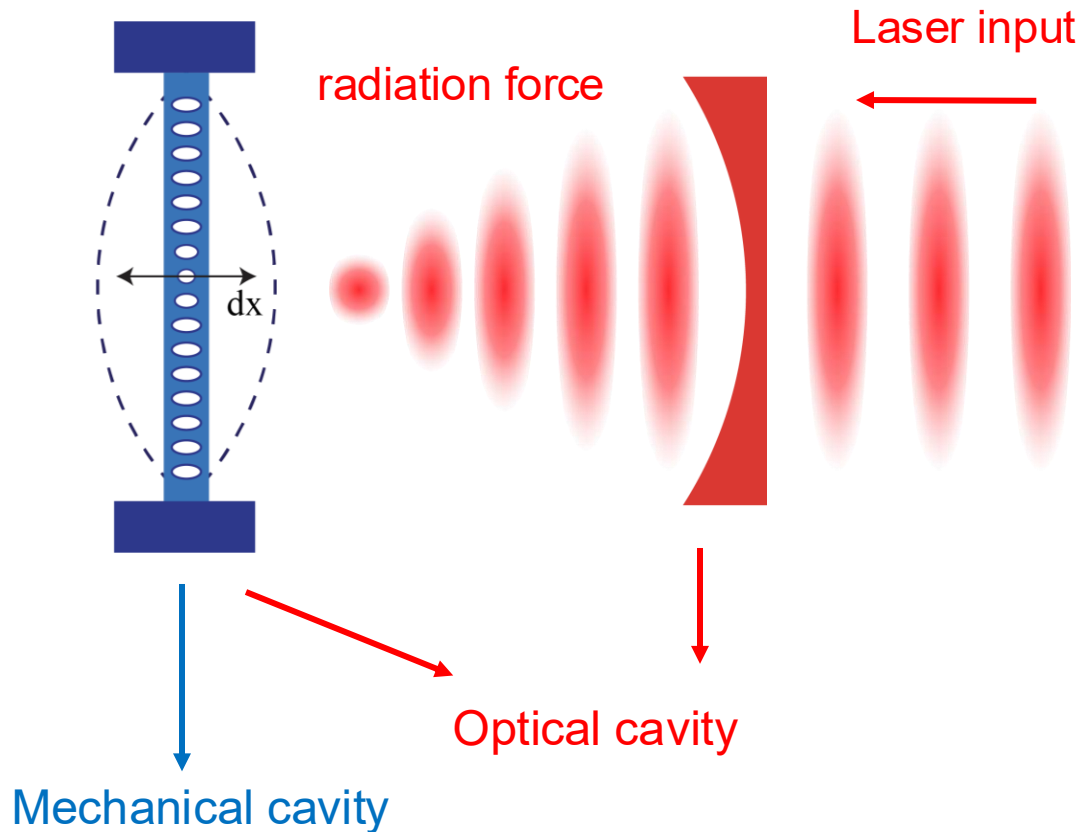
- Requires large photon-phonon interaction area
- Requires high microwave power for 100% mode conversion efficiency

Standing waves:
moving boundary and photoelastic effect



- Cavity-optomechanics
- Cavity-confined optical and acoustic modes

Cavity-optomechanics mw-to-optical transduction



“The radiation pressure of light in the cavity causes the material to deform, which shifts the cavity's resonant frequency.”

$$\omega_{cav}(x) \approx \omega_{cav} + x \frac{\partial \omega_{cav}}{\partial x} + \dots$$

$$\hat{H}_{OM} = \hbar \Omega \hat{b}^\dagger \hat{b} + \hbar \omega_{cav}(x) \hat{a}^\dagger \hat{a} = \hbar \Omega \hat{b}^\dagger \hat{b} + \hbar (\omega_{cav} - G \hat{x}) \hat{a}^\dagger \hat{a}$$

where the coupling coefficient $G \equiv -\frac{\partial \omega_{cav}}{\partial x}$, $\hat{x} = x_{ZPF}(\hat{b} + \hat{b}^\dagger)$

$$\hat{H}_{int} = \hbar g (\hat{b} + \hat{b}^\dagger) \hat{a}^\dagger \hat{a}$$

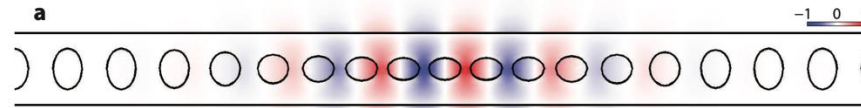
An **optomechanical cavity**

What is “g” exactly?

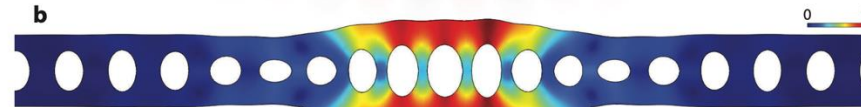
Optomechanical coupling rate g_{om}

Silicon optomechanical cavity

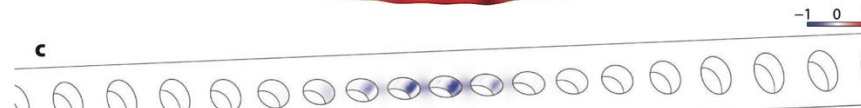
Photonic mode



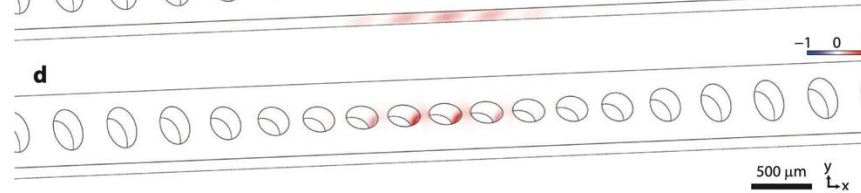
Phononic mode



Photoelastic effect (PE)



Moving boundary effect (MB)



$$g_{OM} = g_{PE} + g_{MB}$$

$$g_{PE} = \left\langle \mathbf{E} \left| \frac{d\varepsilon_{PE}}{du} \right| \mathbf{E} \right\rangle_V \propto (\boldsymbol{\varepsilon} \cdot p\mathbf{S} \cdot \boldsymbol{\varepsilon}) \propto n^4$$

$$g_{MB} = \left\langle \mathbf{E} \left| \frac{d\varepsilon_{MB}}{du} \right| \mathbf{E} \right\rangle_S \propto (\Delta\varepsilon' |\mathbf{E}_{\parallel}|^2 - \Delta\varepsilon'^{-1} |\mathbf{D}_{\perp}|^2)$$

PE: Bulk effect

- Photoelastic coefficient tensor (p)
- Strain tensor (\mathbf{S})

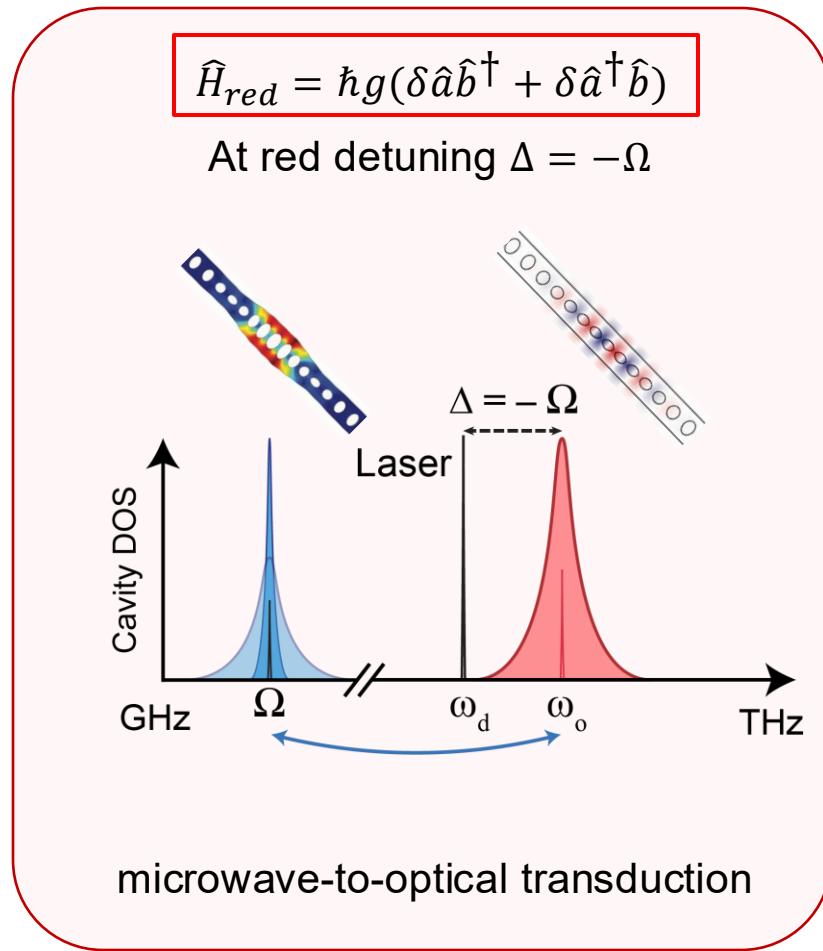
MB: Surface effect

- tangential electric field (\mathbf{E}_{\parallel})
- normal displacement field (\mathbf{D}_{\perp})

How to use this to convert microwave signal to optical?

Cavity-optomechanics mw-to-optical transduction

By H_{int} linearization ($\hat{a} \rightarrow \bar{a} + \delta\hat{a}$) and rotating-wave approximation at the lab frame (discarding 2Ω terms)



Microwave-frequency *photons*
from superconducting qubits \hat{c}

Electromechanical
transducer

**Piezoelectric
material**

Microwave mechanical modes \hat{b}

Red detuned laser pump

$\hat{H}_{red} = \hbar g(\delta\hat{a}\hat{b}^\dagger + \delta\hat{a}^\dagger\hat{b})$

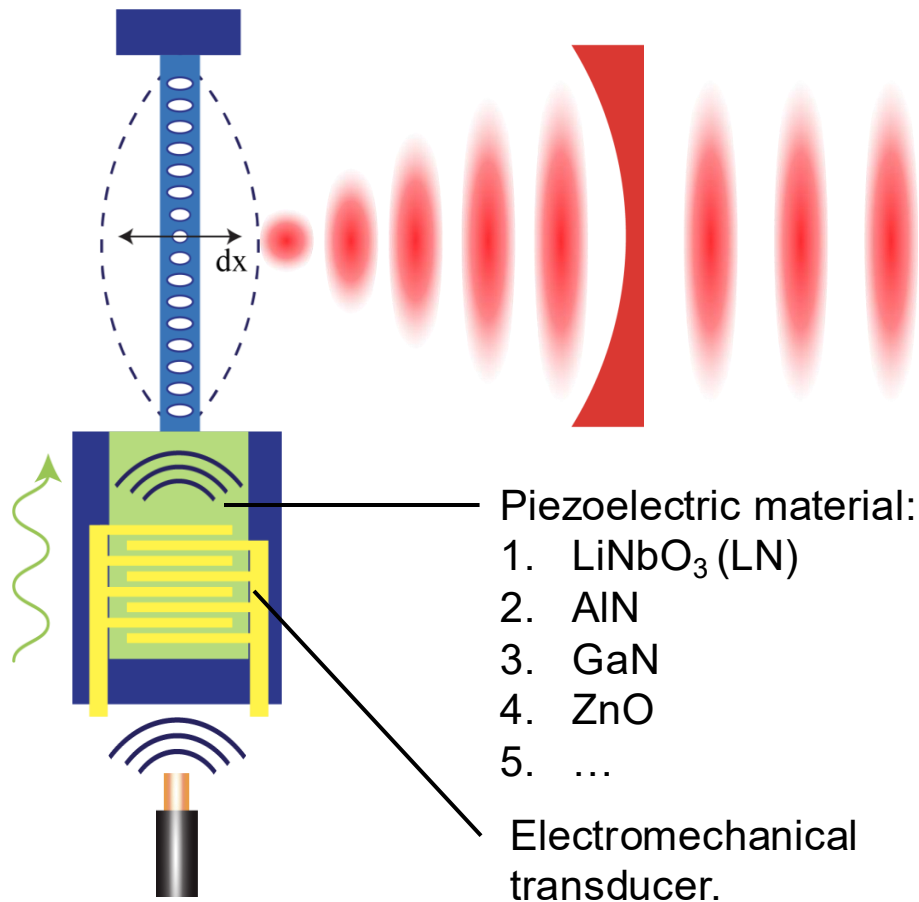
in an optomechanical cavity

Terahertz optical modes \hat{a}

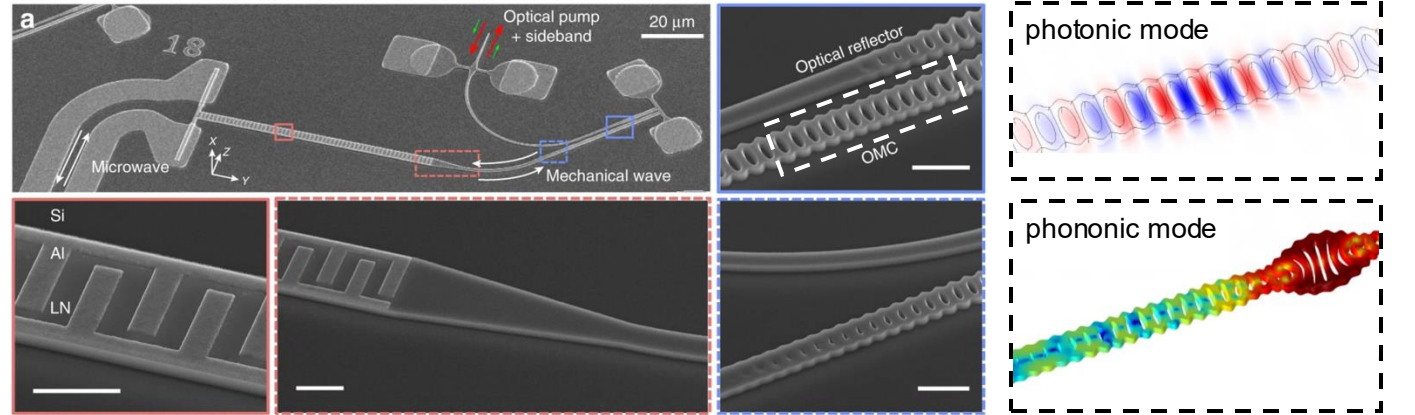
Sound (phonons) \rightarrow Optical signal (photons)

Cavity-optomechanics microwave-to-optical transduction

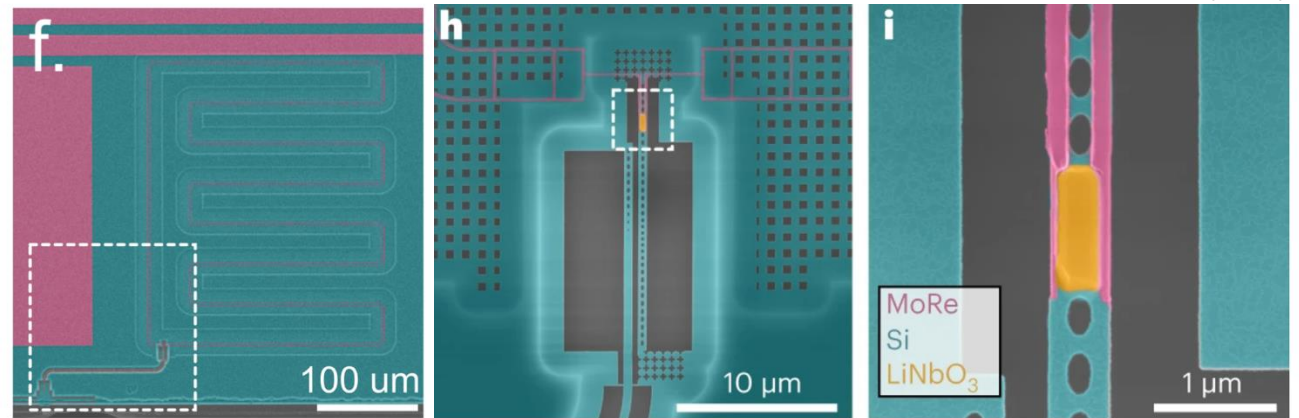
Optomechanical cavity (OMC)



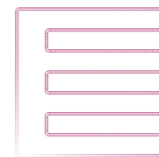
OMC + Piezoelectric material: LiNbO_3



LiNbO_3 -on-Si



microwave photonic mode



phononic mode



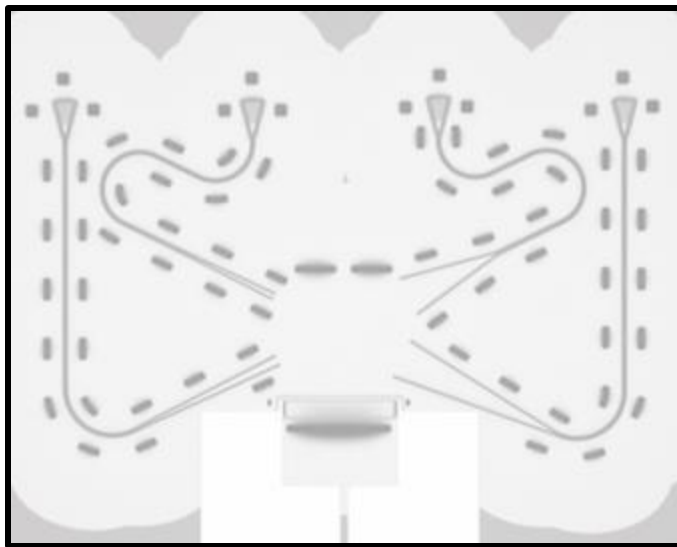
optical photonic mode



Overview

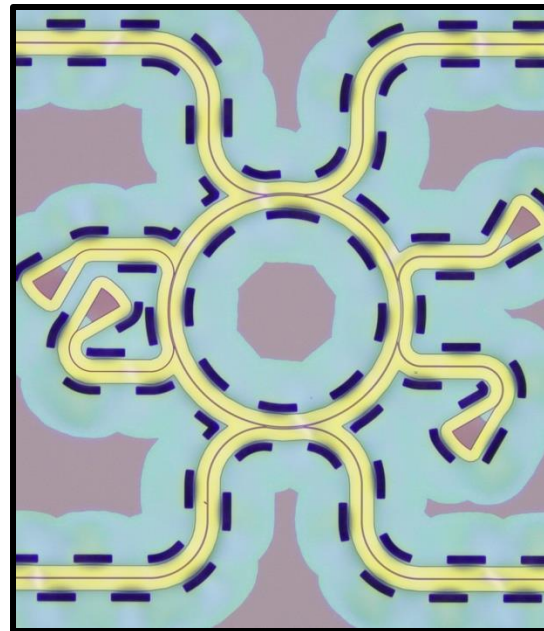
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Acousto-optics frequency shifter (AOFS)

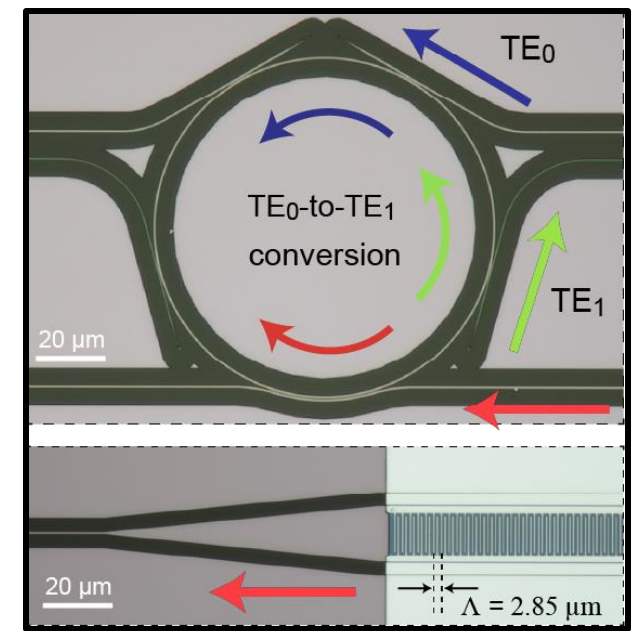


N. S. Yama*, I.-T. Chen* et al., *Advanced Materials* (2023)

Microwave-to-optical transduction



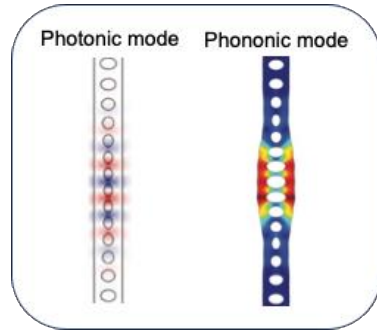
I.-T. Chen et al., *Nat. Commun.* (2023)



I.-T. Chen et al., submitted (2025)

Optomechanical Integrated Circuit Coupling Rate g_{OMIC}

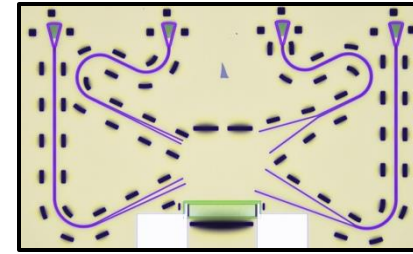
Standing waves:
Cavity-optomechanics
Two-mode coupling: \hat{a} and \hat{b}



$$g_{OM} = g_{PE} + g_{MB}$$

Cavity-optomechanics

Traveling waves:
Brillouin scattering
Three-mode coupling: \hat{a}_0 , \hat{a}_1 and \hat{b}



$$\vec{\beta}_0 \pm \vec{q} = \vec{\beta}_1$$

$$\omega_0 \pm \Omega = \omega_1$$

Brillouin Scattering

$$= g_{OMIC} = \underbrace{\left(\left\langle \mathbf{E}_0 \left| \frac{d\varepsilon_{PE}}{du} \cdot \mathbf{u} \right| \mathbf{E}_1 \right\rangle_V + \left\langle \mathbf{E}_0 \left| \frac{d\varepsilon_{MB}}{dx} \cdot \mathbf{u} \right| \mathbf{E}_1 \right\rangle_S \right)}_{\text{PE MB}} \cdot \underbrace{\exp^{-i(\vec{\beta}_0 \pm \vec{q} \mp \vec{\beta}_1)r} \cdot \exp^{-i(\omega_0 \pm \Omega \mp \omega_1)t}}_{\text{Phase-matching condition}}$$

Phonon \rightarrow photon when phase-matching conditions is satisfied

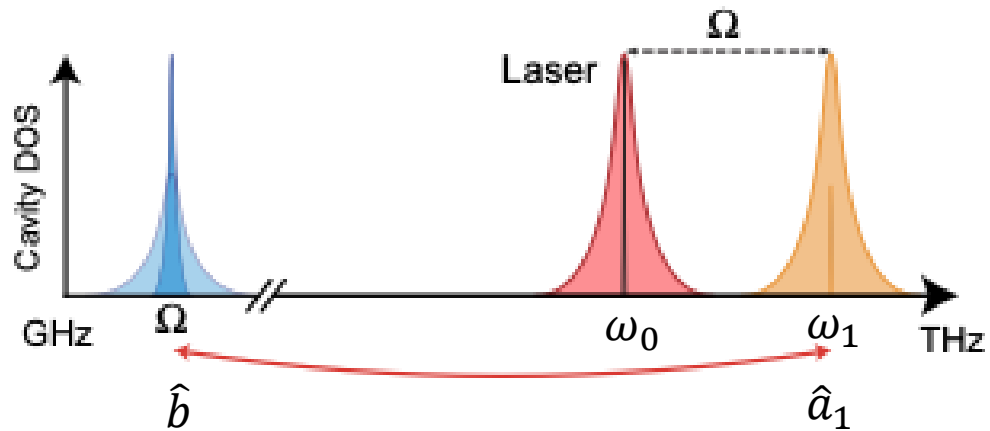
Building block for interconnecting qubits

$$\hat{H}_{int} = \hbar g_{OMIC}' \left(\hat{a}_0^\dagger \hat{a}_1 \hat{b}^\dagger + \hat{a}_0 \hat{a}_1^\dagger \hat{b} \right) \exp^{-i(\vec{\beta}_0 \pm \vec{q} \mp \vec{\beta}_1)r} \cdot \exp^{-i(\omega_0 \pm \Omega \mp \omega_1)t} + h.c.,$$

When the PMC are satisfied: $\vec{\beta}_0 + \vec{q} = \vec{\beta}_1$

- When laser drives: $\hat{a}_0 \rightarrow \langle \hat{a}_0 \rangle$,

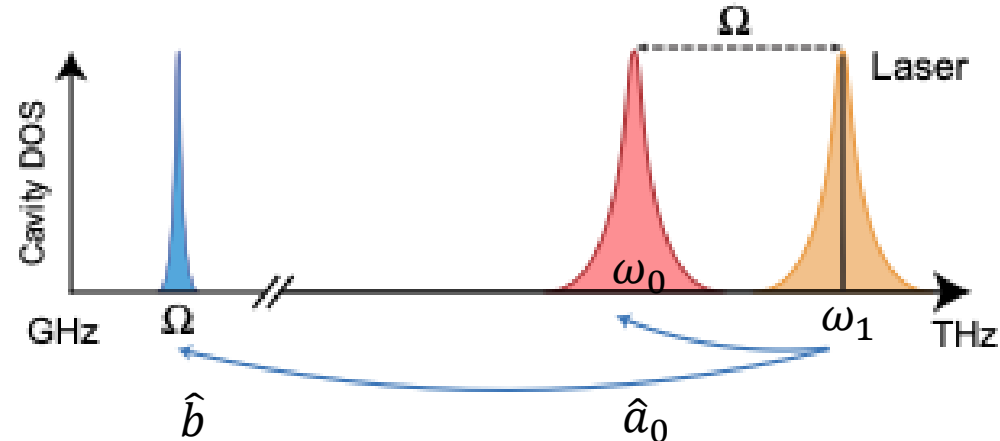
$$\hat{H}_{red} = \hbar G_0 (\hat{a}_1 \hat{b}^\dagger + \hat{a}_1^\dagger \hat{b}) \quad G_0 = g_{OMIC} \langle \hat{a}_0 \rangle$$



microwave phonon ↔ optical transduction

- When laser drives: $\hat{a}_1 \rightarrow \langle \hat{a}_1 \rangle$,

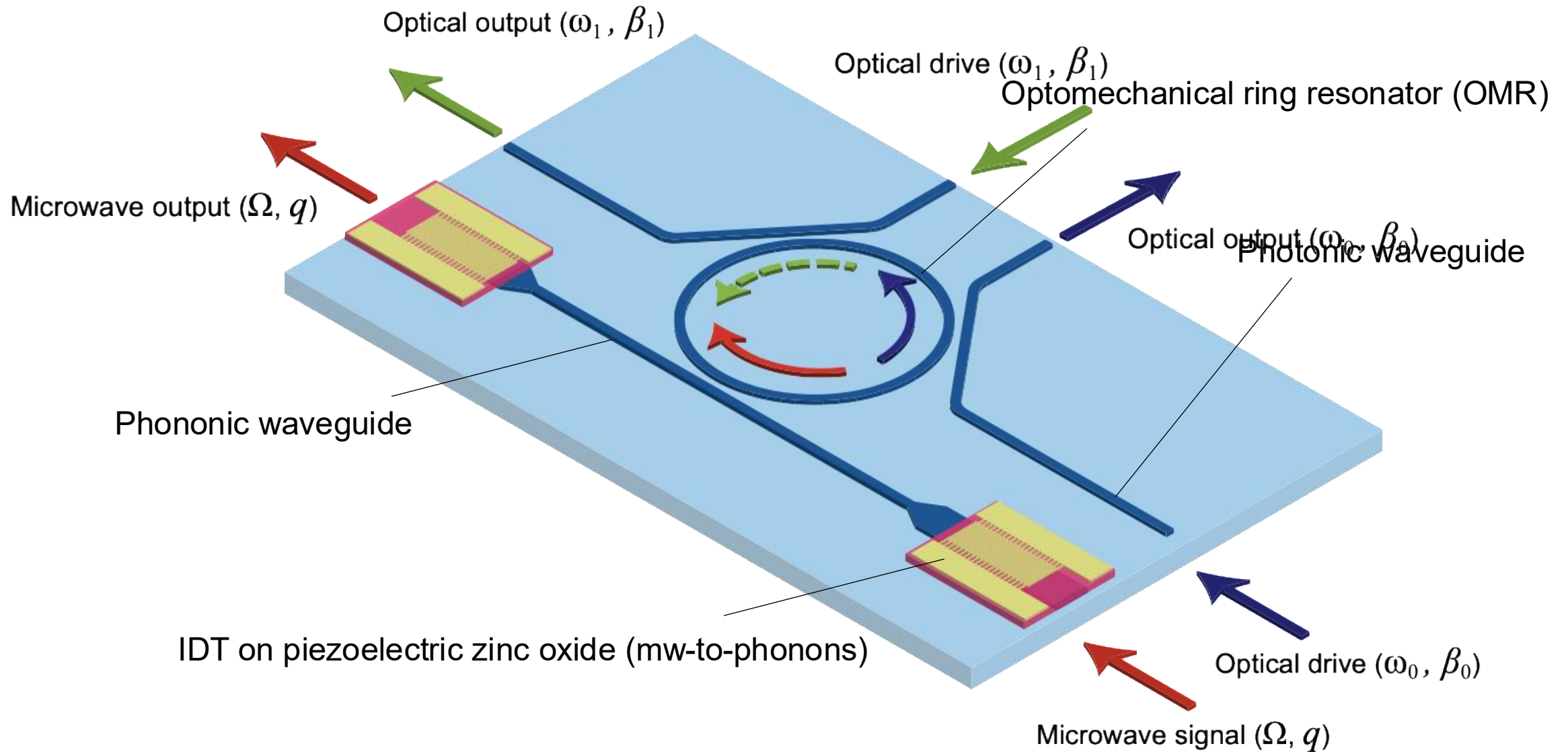
$$\hat{H}_{blue} = \hbar G_1 (\hat{a}_0^\dagger \hat{b}^\dagger + \hat{a}_0 \hat{b}) \quad G_1 = g_{OMIC} \langle \hat{a}_1 \rangle$$



microwave phonon ↔ optical entanglement

By selecting a drive optical mode →
select transduction or entanglement generation

Realizing Optomechanical Integrated Circuits (OMIC)



$$\hat{H}_{\text{blac}} = \hbar\omega_0(\hat{a}_0^\dagger\hat{b} + \hat{a}_0\hat{b}^\dagger)$$

Material requirements

Material requirements for optomechanical integrated circuits

- Acoustic wave guiding: low acoustic velocity (v)
- Optical wave guiding: high refractive index (n)
- Strong optomechanical interaction: high photoelastic coefficient (p)
- Can convert microwave signal to acoustic wave: piezoelectricity

$$\text{Acousto-optic figure-of-merit: } M_2 = \frac{p^2 n^6}{\rho v^3}$$

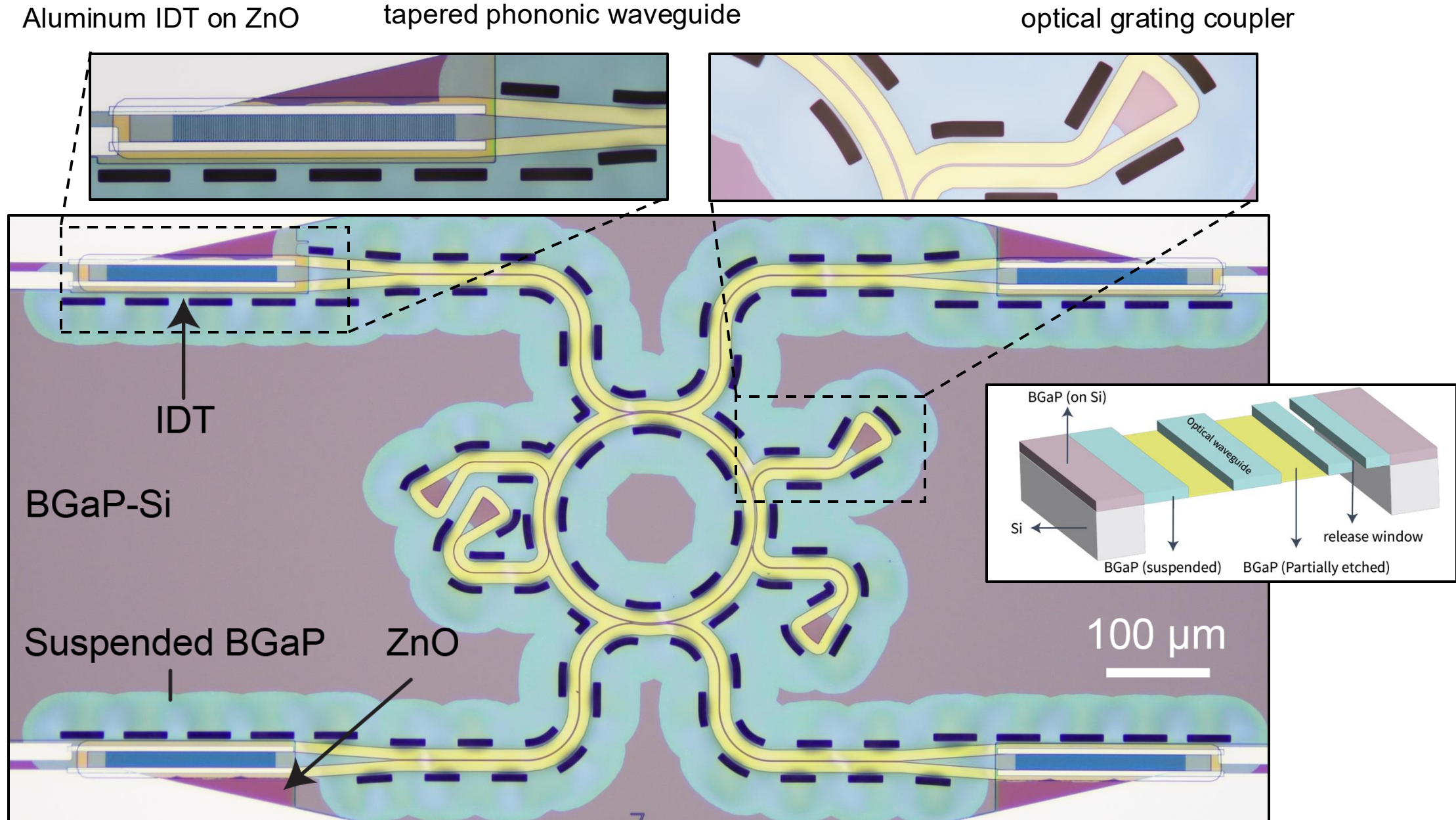
($\times 10^{-15}$)

	k_{em}^2 (%)	n (1.55 μm)	p_{ij}	ρ (g/cm^3)	v_s (m/s)	M_2 ($s^3 kg^{-1}$)
AlN	7.2	2.19	$p_{11} = -0.1$	3.26	5760	1.7
GaAs	0.38	3.37	$p_{11} = -0.16$	5.32	4726	66.7
GaN	1.3	2.31	$p_{11} = -0.09$	6.15	3941	3.26
GaP	0.2	3.05	$p_{11} = 0.151$ [32]	4.13	4100	64.5
LiNbO ₃	17.2	2.21	$p_{31} = 0.172$ [32]	4.64	3978	11.8
Si*	0	3.47	$p_{11} = -0.095$ (RT) -0.160 (5K)	2.33	5845	36.1
ZnO	3.3	1.92	$p_{11} = -0.2$	5.61	3500	8.3

(Y-cut)

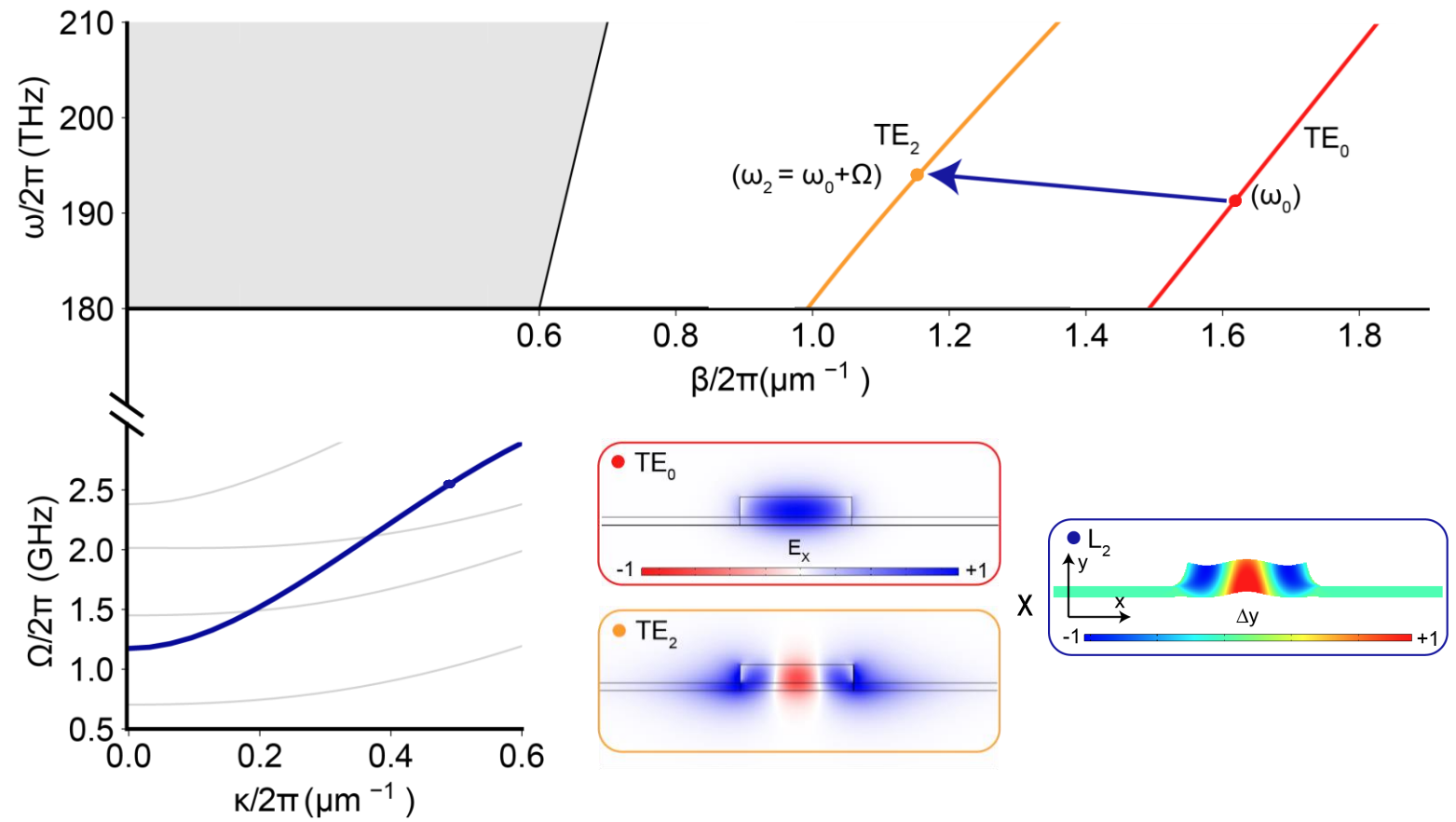
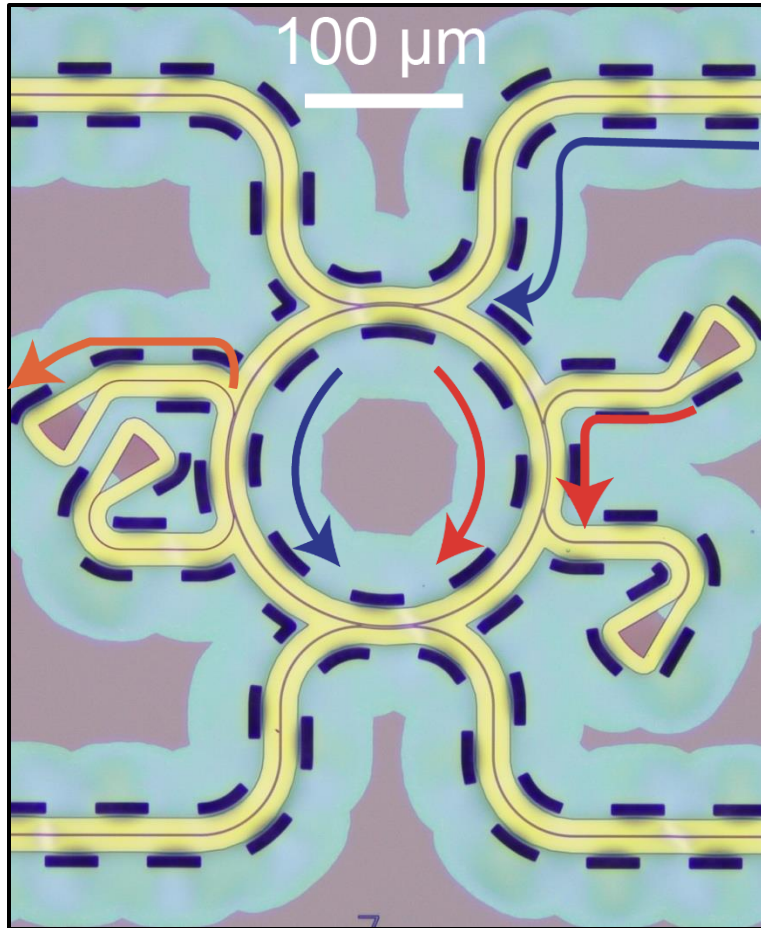


Experimental realization: OMIC on BGaP

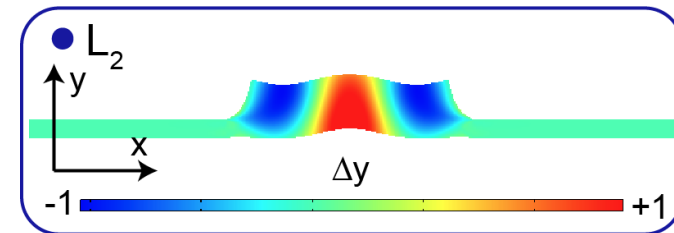
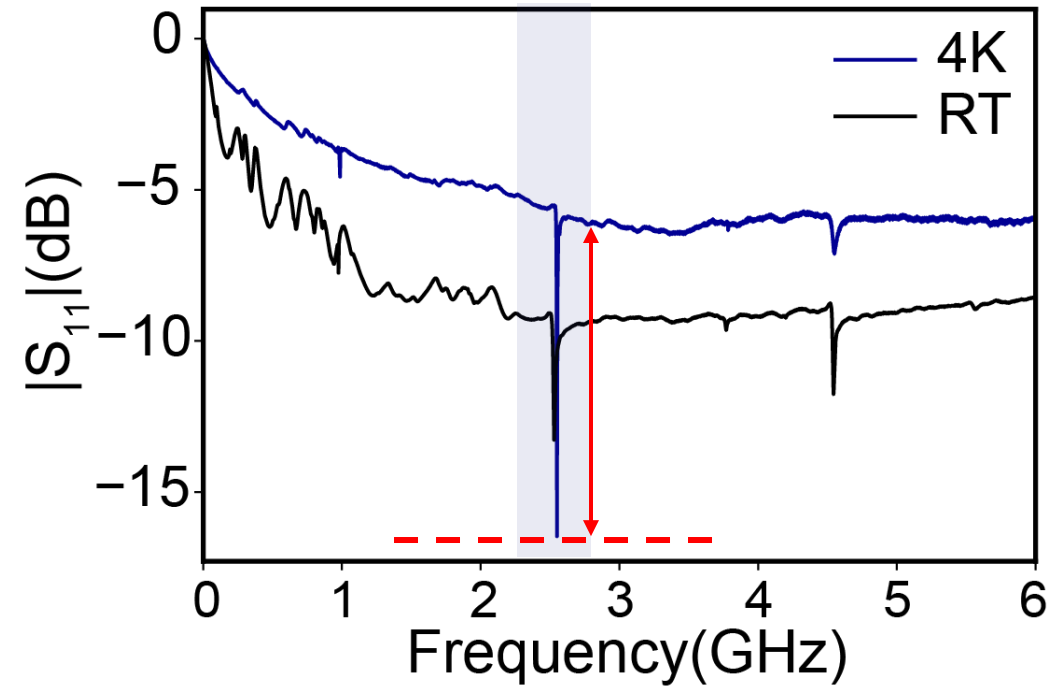
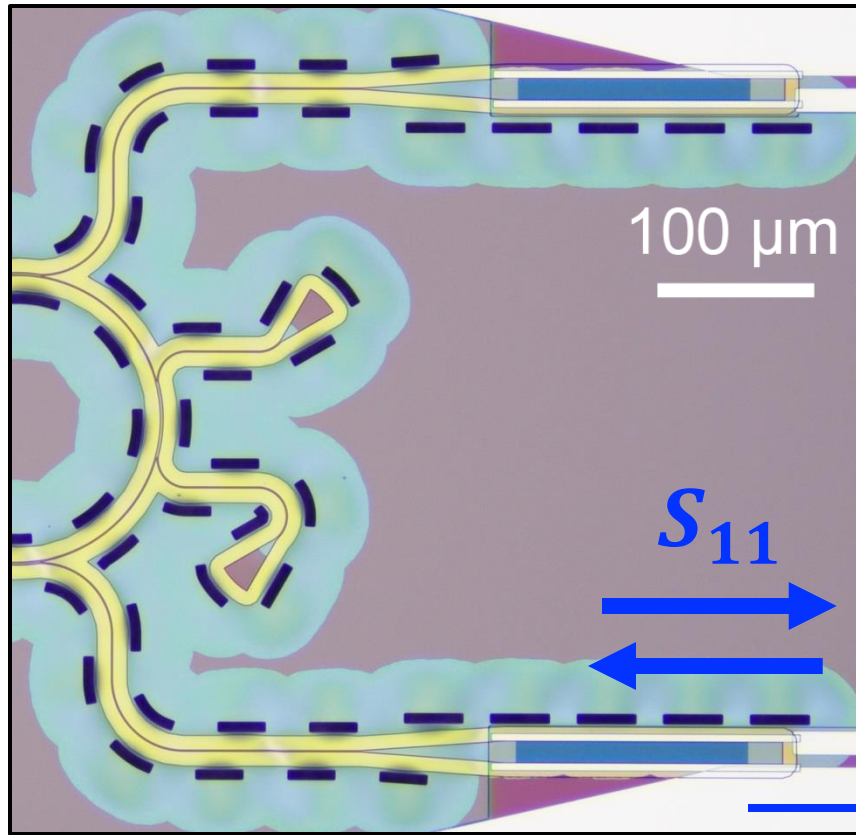


Phase-matching condition in OMR

Three modes propagates in OMIC

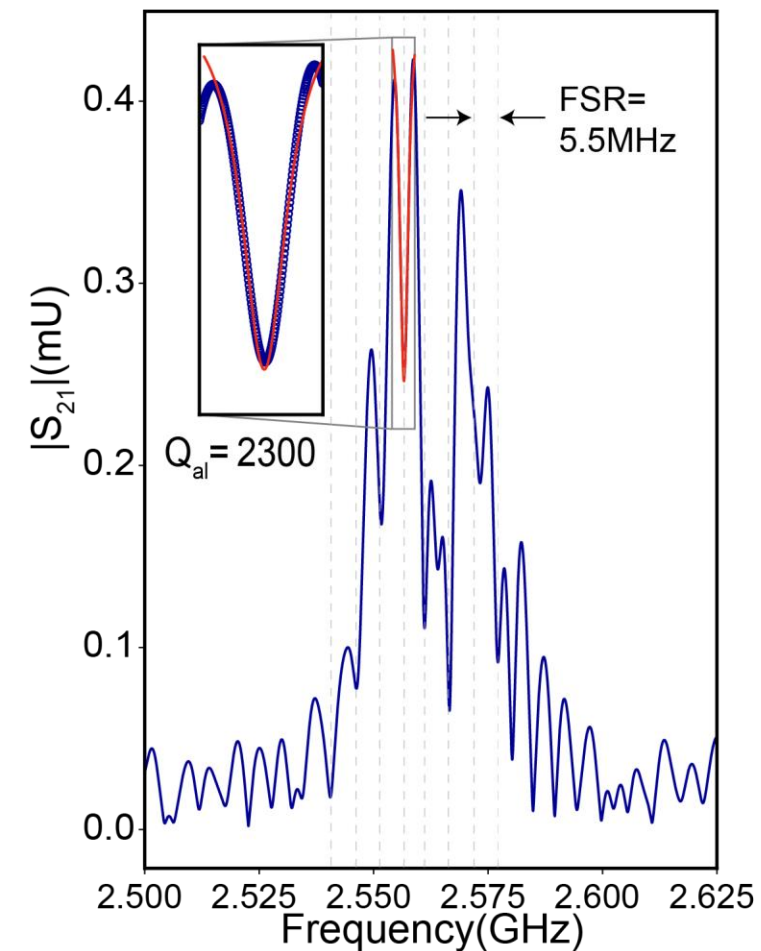
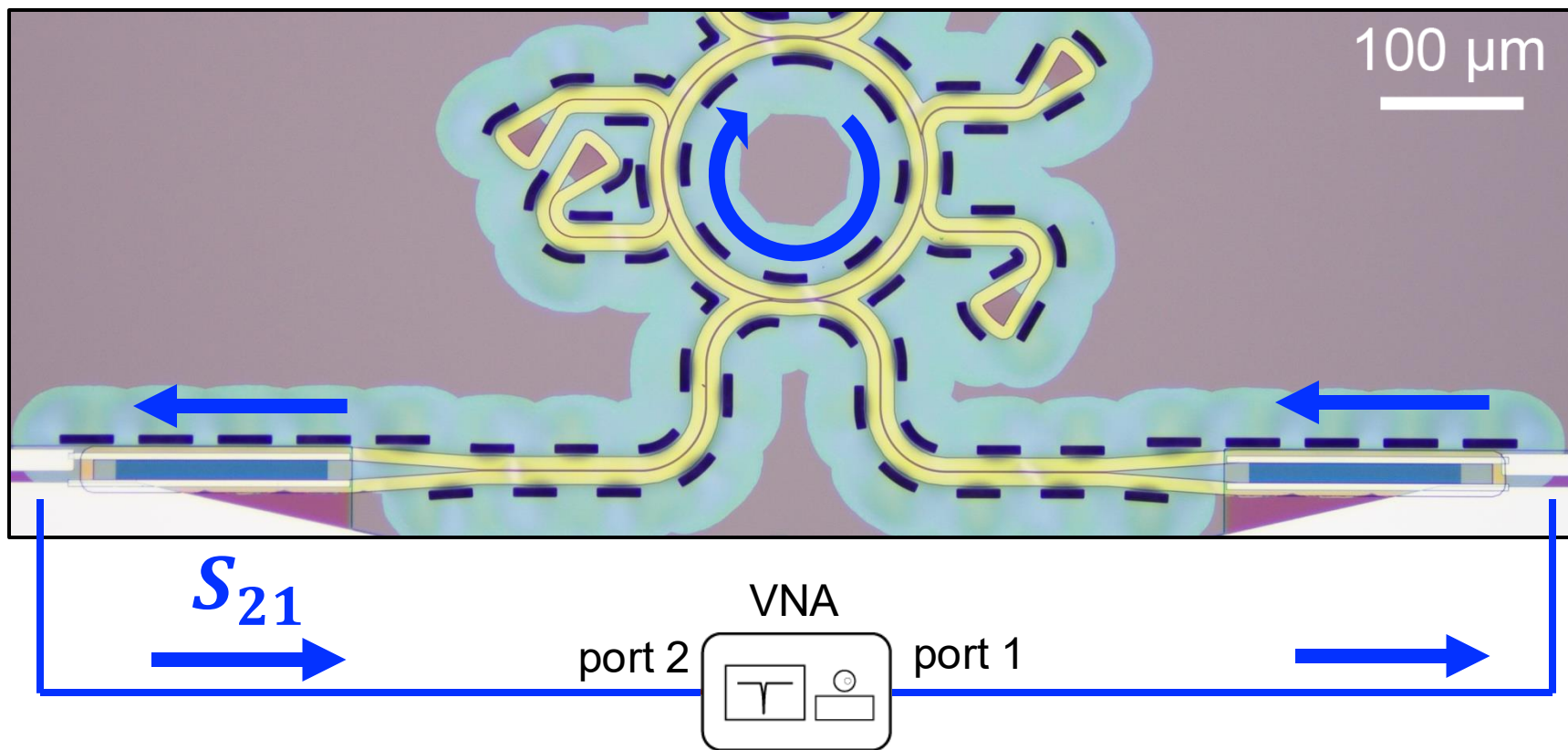


Phononic modes characterization: reflection coefficient



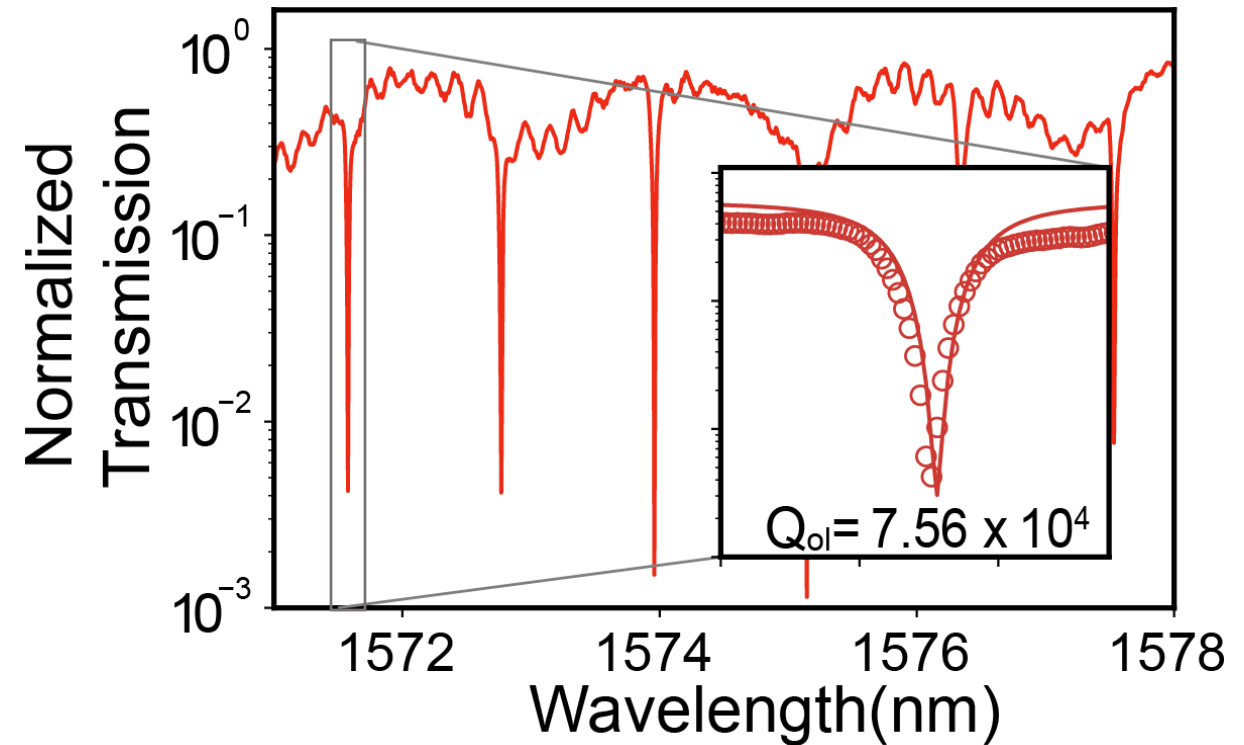
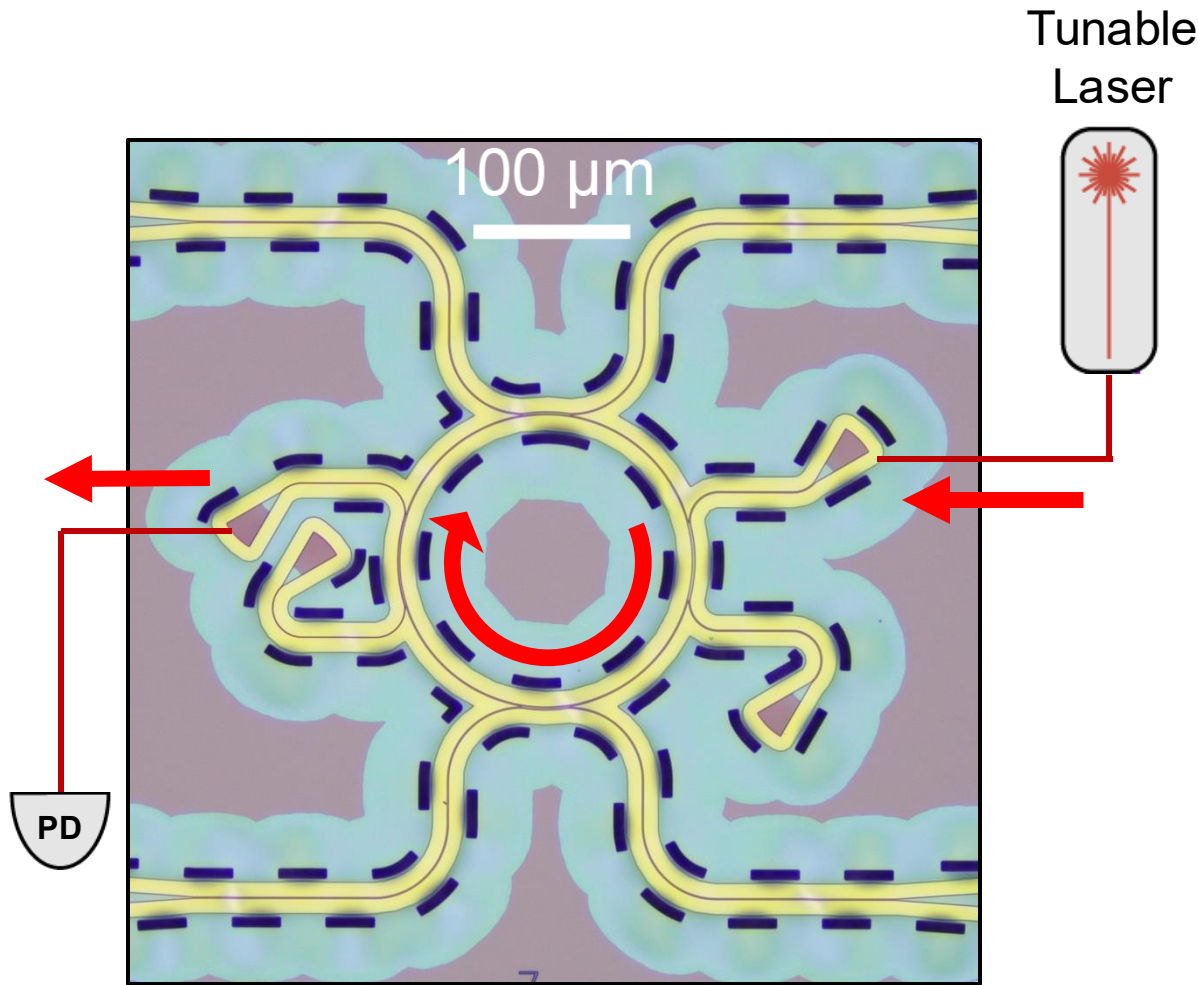
Microwave to phononic mode efficiency $\eta_{em} > 90\%$ at 4K by modified-BVD model

Phononic modes characterization: transmission coefficient



Multi-phononic resonances circulating in the OMR.
Loaded quality factor: $Q_a \sim 2300$

Photonic characterizations



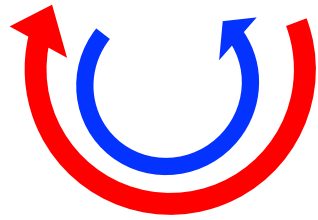
Loaded optical quality factor: $Q_o \sim 75,000$

Device characterization: Time-reversal symmetry

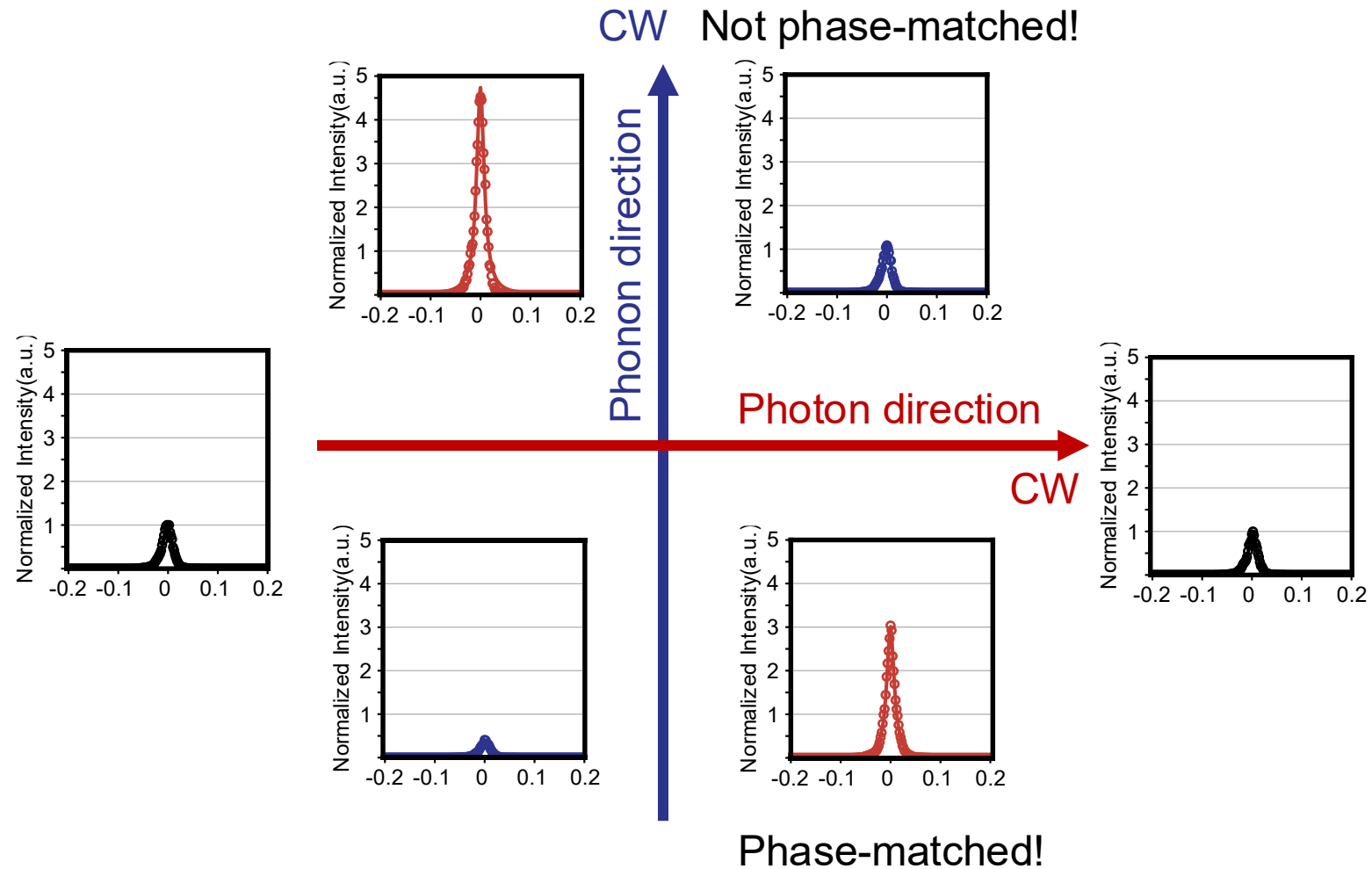
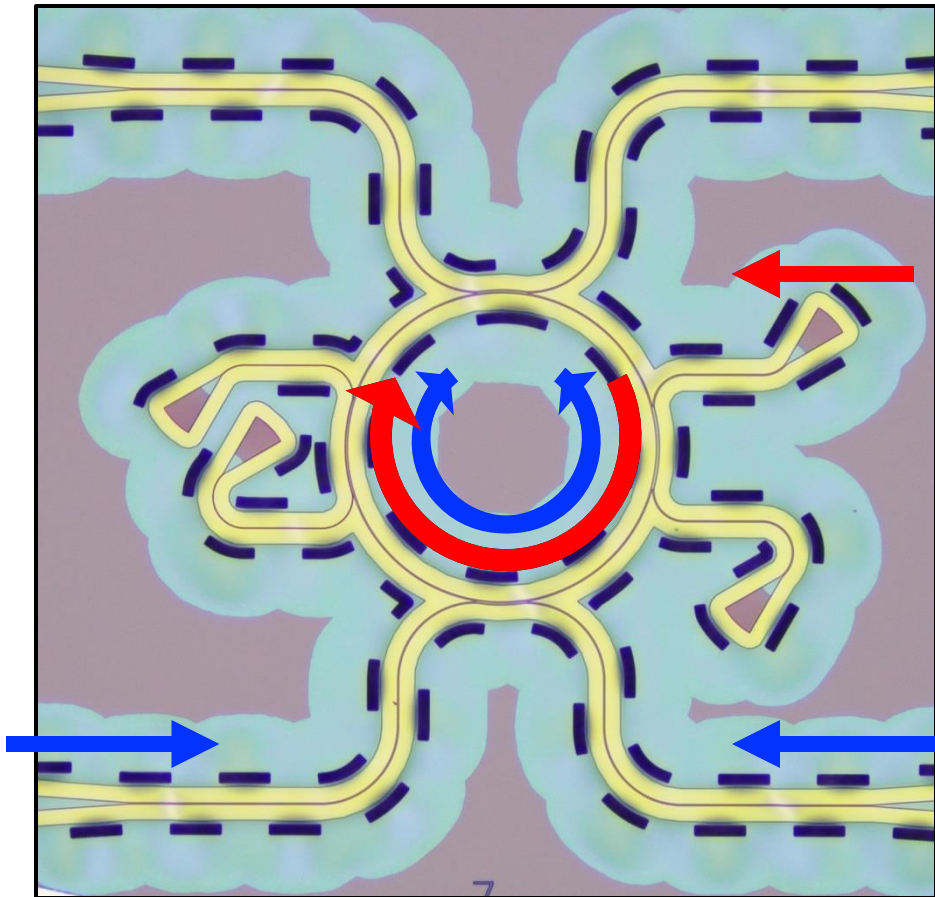
Phase-matching condition:

$$\vec{\beta}_0 - \vec{q} + \vec{\beta}_1 = 0$$

(+): clock-wise



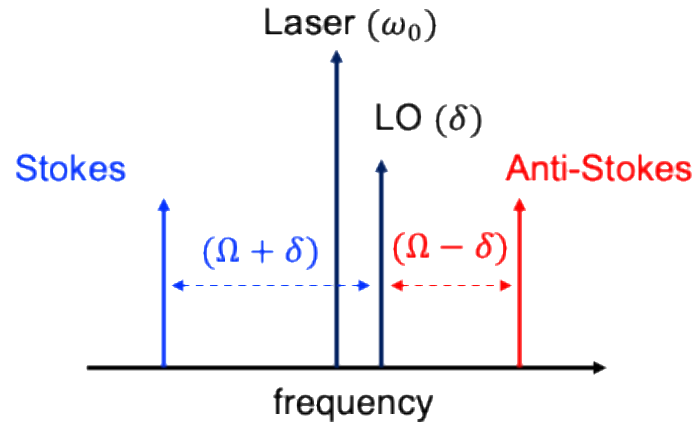
Output intensity received by an optical spectrum analyzer (OSA)
(fixed optical drive)



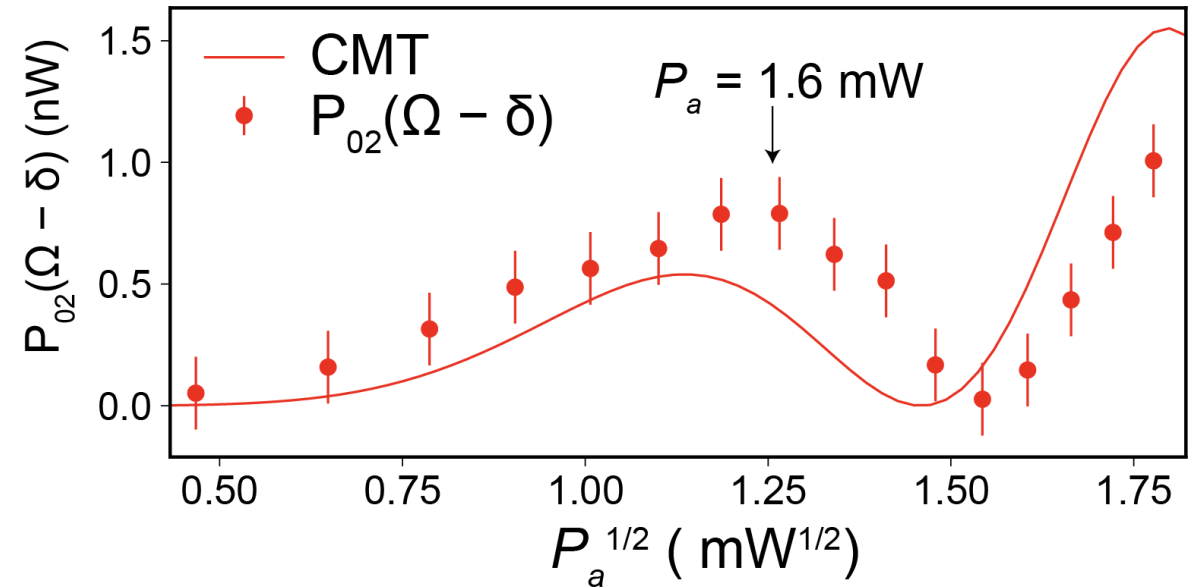
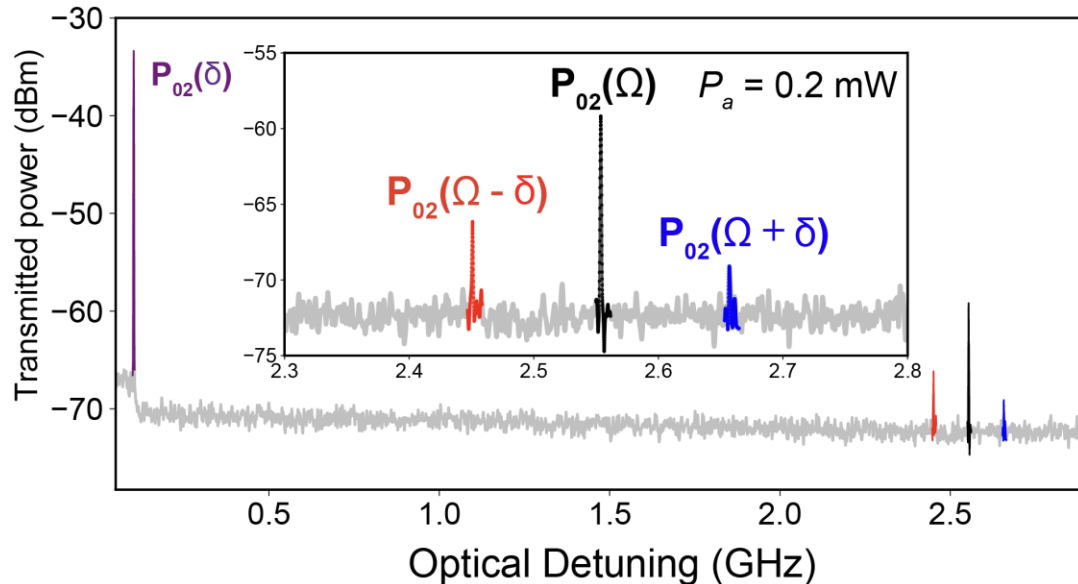
This indicates optomechanical coupling in OMIC

Frequency resolved optical spectrum

Optical heterodyne measurements



Beating signal in the optical spectrum



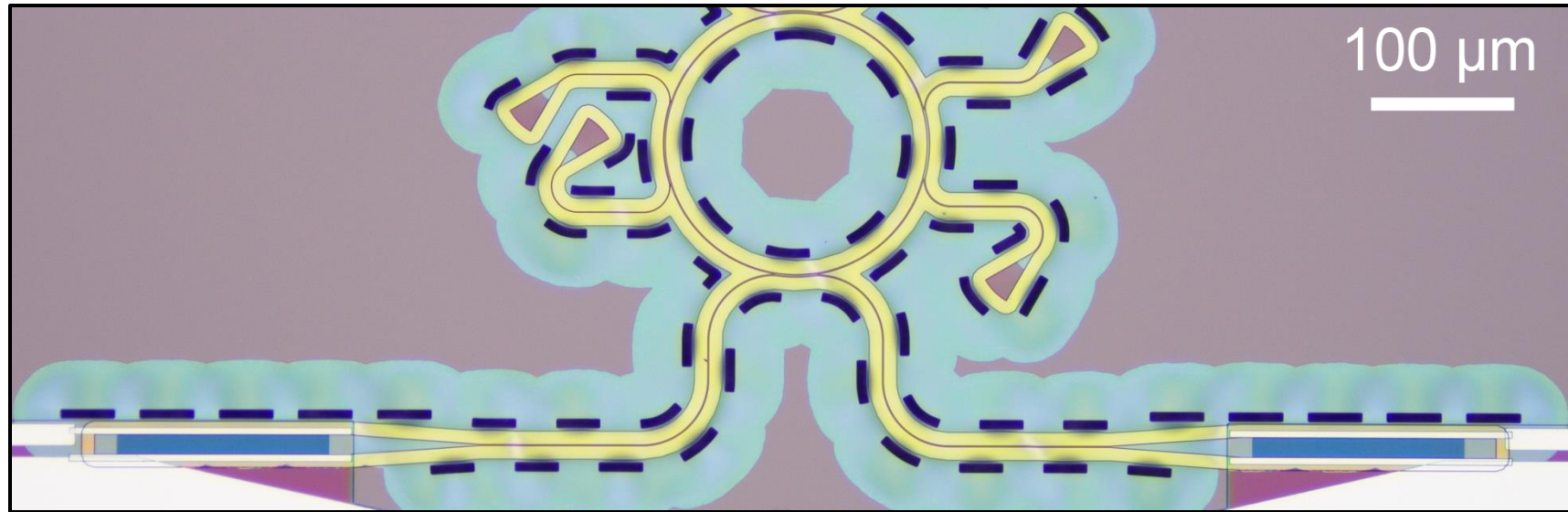
Coupled mode theory fitting (CMT):

$$A_2(z) = A_0(0) \left[-iG \frac{\sin(sz)}{s} \right] e^{i\Delta\beta z/2}$$

Oscillatory features: traveling wave cavity + multi-mode

microwave \rightarrow phonons (Lamb mode) \rightarrow optical (TE_2)

Summary on the first OMIC

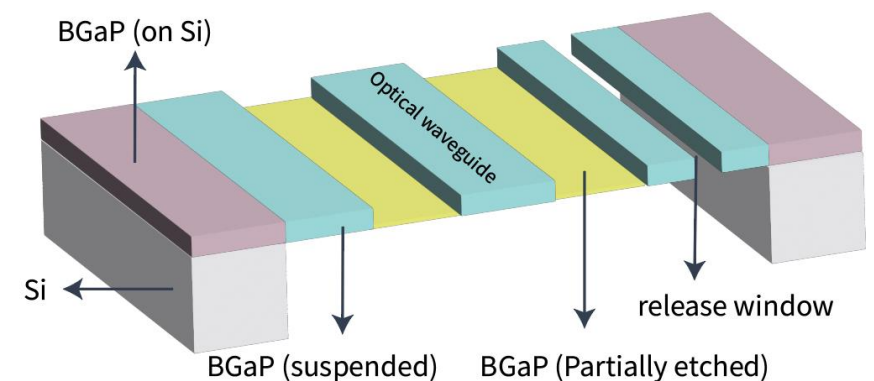


Feature:

- The first optomechanical integrated circuit (OMIC) and ring resonator (OMR)
- On a suspended BGaP thin film
- This is a hybrid platform: ZnO and BGaP

Problems:

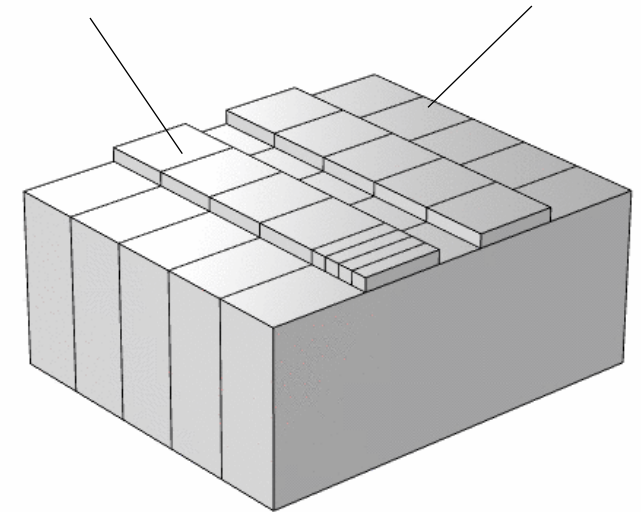
- Suspended
 - Difficult to integrate with SC qubits
 - Optical induced heating limits the efficiency



Silicon-on-sapphire (SOS)

- Phononic waveguiding ($v_{si} \sim 5000 \text{ m/s}$ vs. $v_{sapp.} \sim 10,000 \text{ m/s}$)
- Photonic waveguiding ($n_{si} \sim 3.4 @ 1.55 \mu\text{m}$ vs. $n_{sapp.} \sim 1.72 @ 1.55 \mu\text{m}$)
- Compatible with silicon integrated photonics
- Compatible with many quantum platforms
 - Single photon source at 1.27 μm : G-centers^[1]
 - Millisecond coherence superconducting qubits^[2]

Silicon waveguide Sapphire



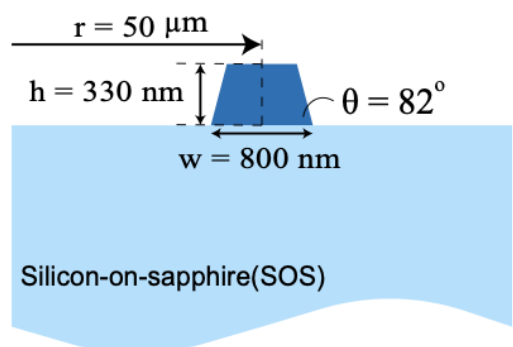
SOS phononic waveguiding

An ideal platform for optomechanical integrated circuits (OMIC)

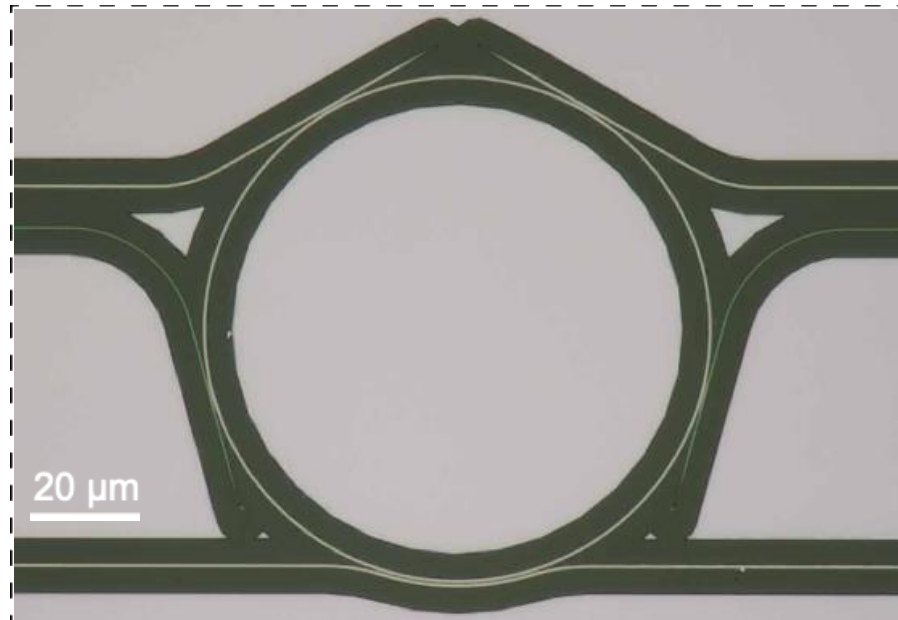
[1] W. Redjem et al., *Nature Electronics*, 3(12), 738-743. (2020)

[2] A. Somoroff et al., *Phys. Rev. Lett.* 130, 267001 (2023)

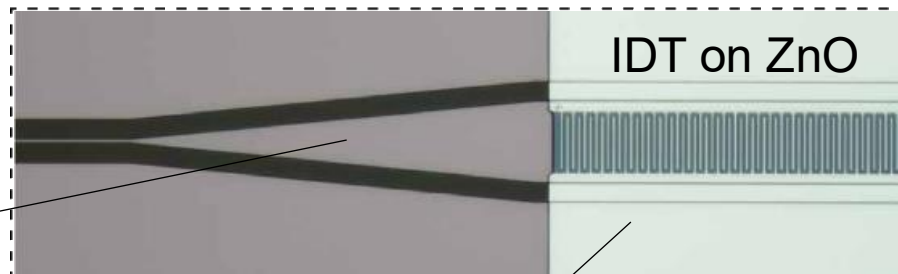
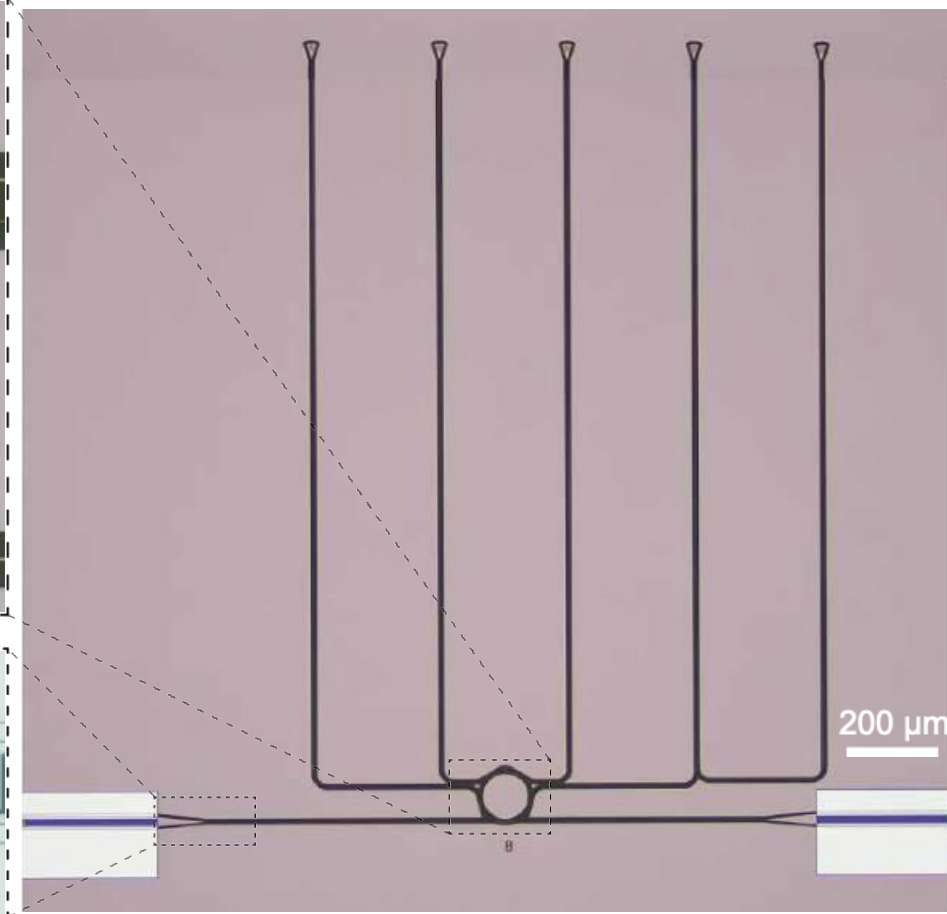
OMIC on silicon-on-sapphire (SOS)



OMR



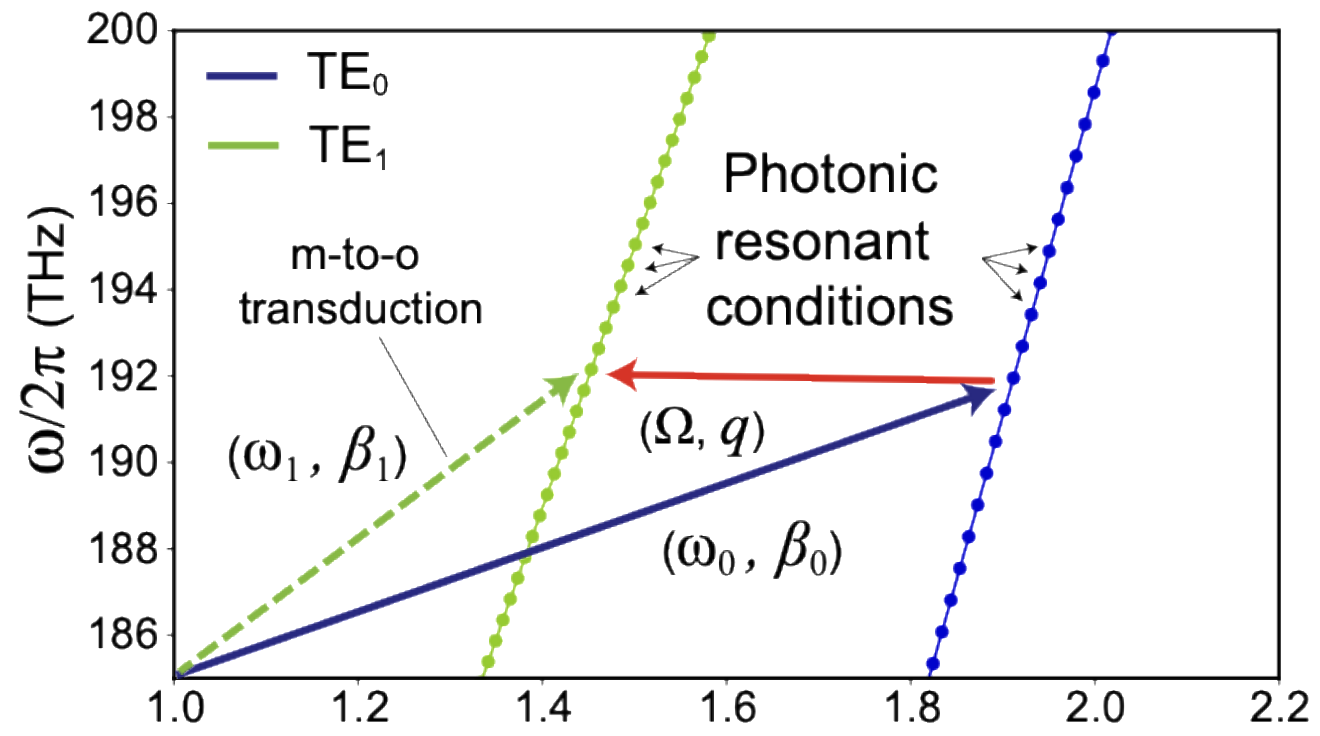
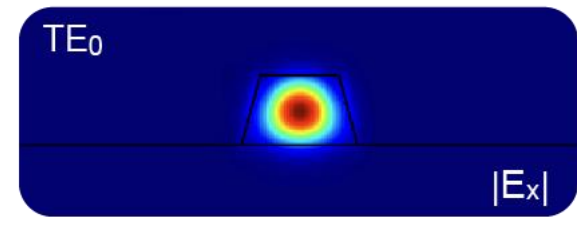
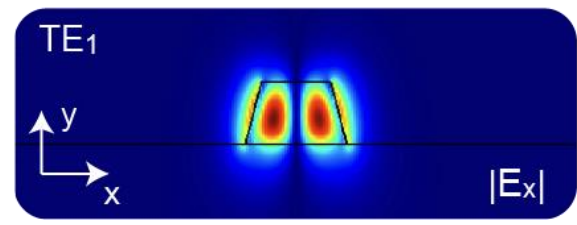
OMIC on SOS



Phononic waveguide

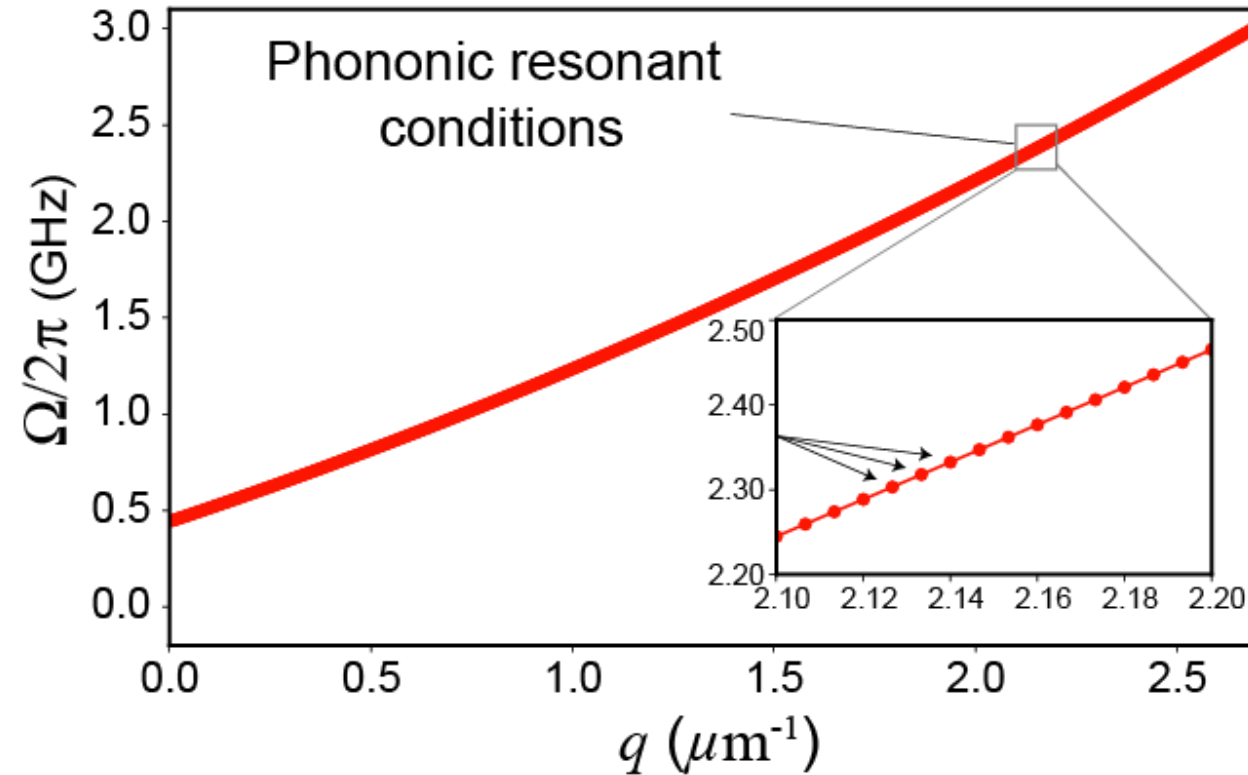
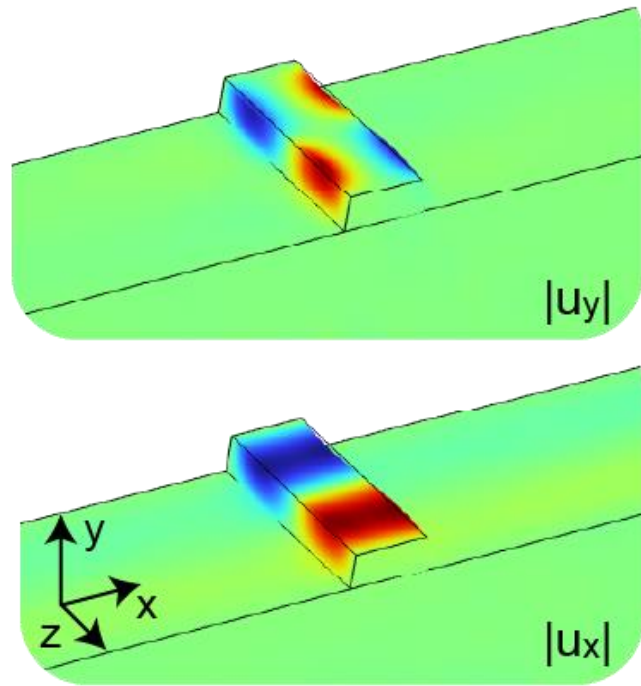
Silicon is not piezoelectric, so a ZnO thin film is deposited to excite phononic mode.

Phase-matching condition



$$\hat{H}_{red} = \hbar G_{OMIC} (\hat{a}_1 \hat{b}^\dagger + \hat{a}_1^\dagger \hat{b})$$

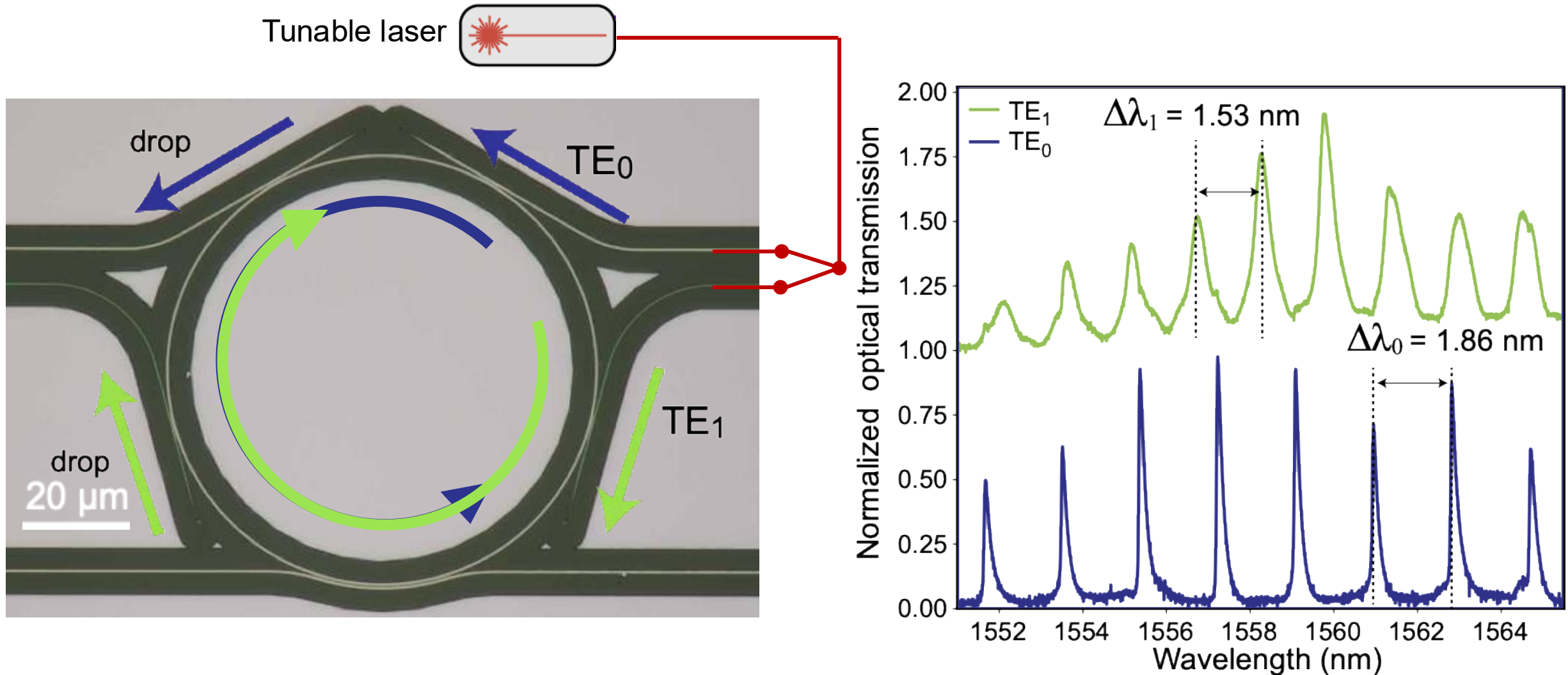
Phononic waveguide resonances



- First-order Love mode (L_0)
- Dispersion curve of the phononic modes in OMR, dots are resonances

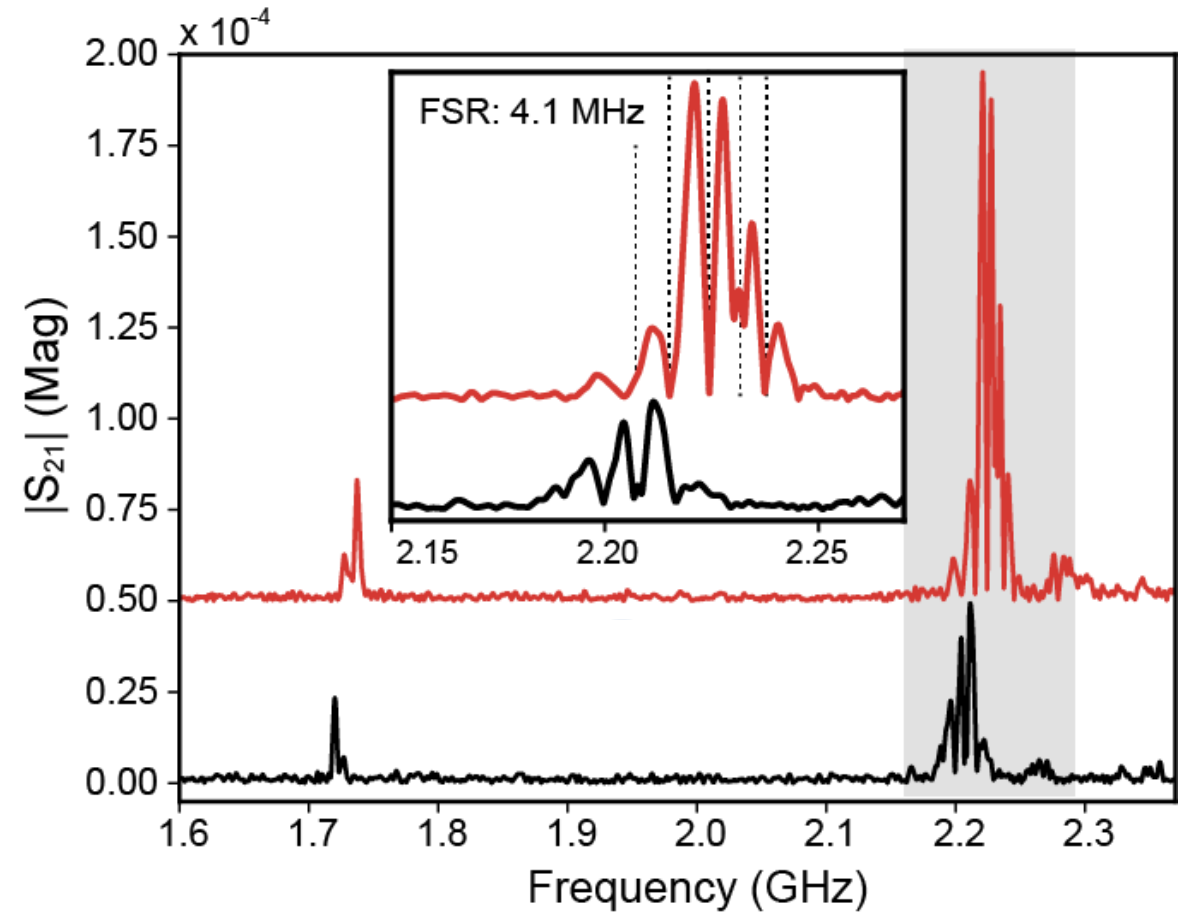
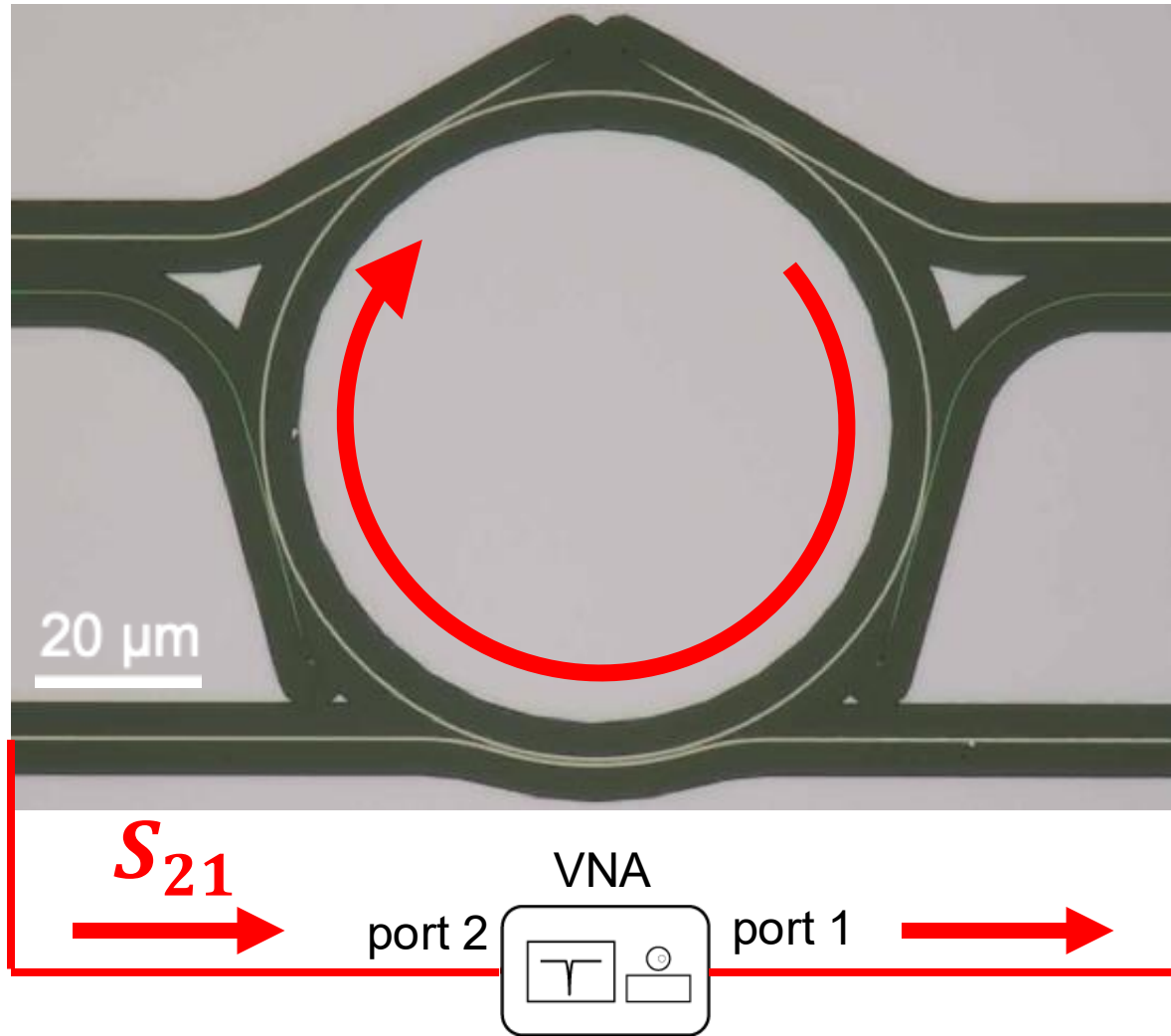
Photonic resonance characterization

- Two pairs of waveguides (different widths) are used to selectively drive the photonic modes TE_0 and TE_1



- Intrinsic quality factor $Q_0 = 100K$, $Q_1 = 8K$

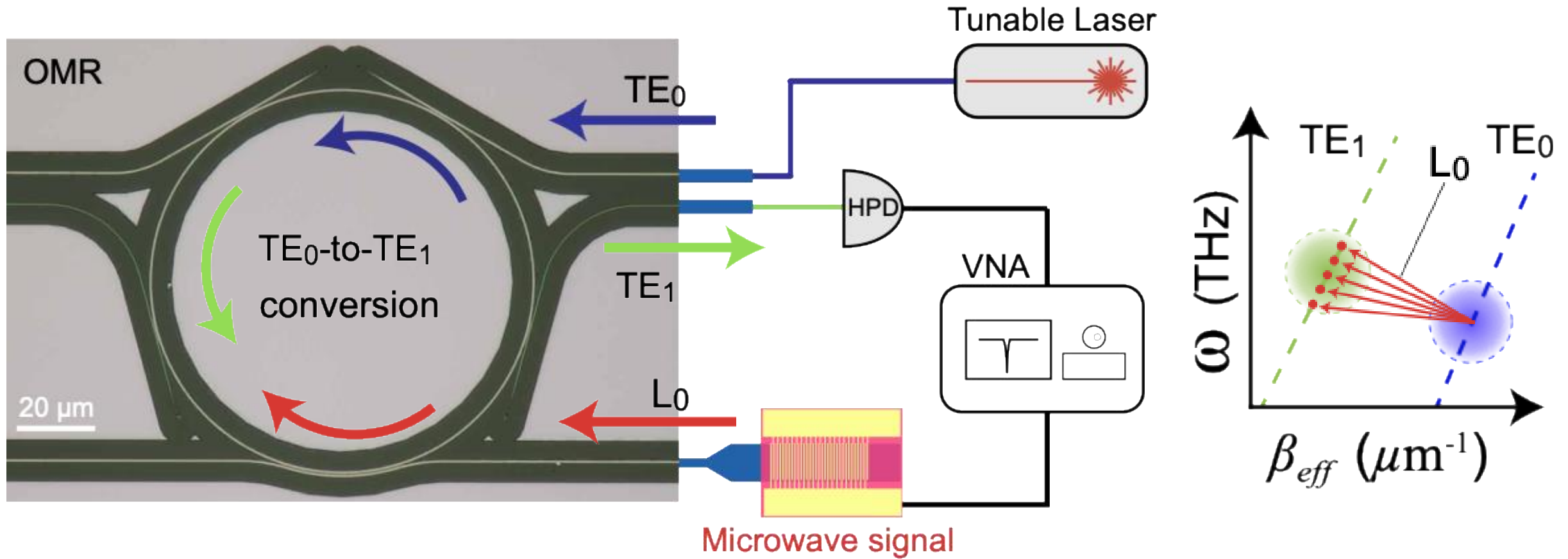
Photonic resonance characterization



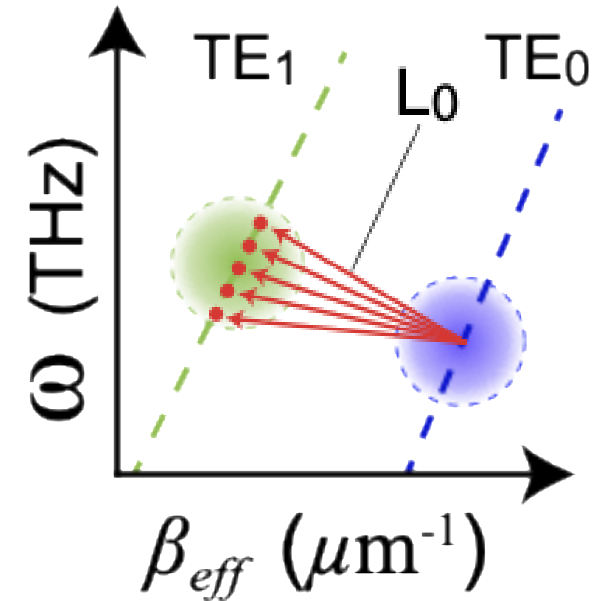
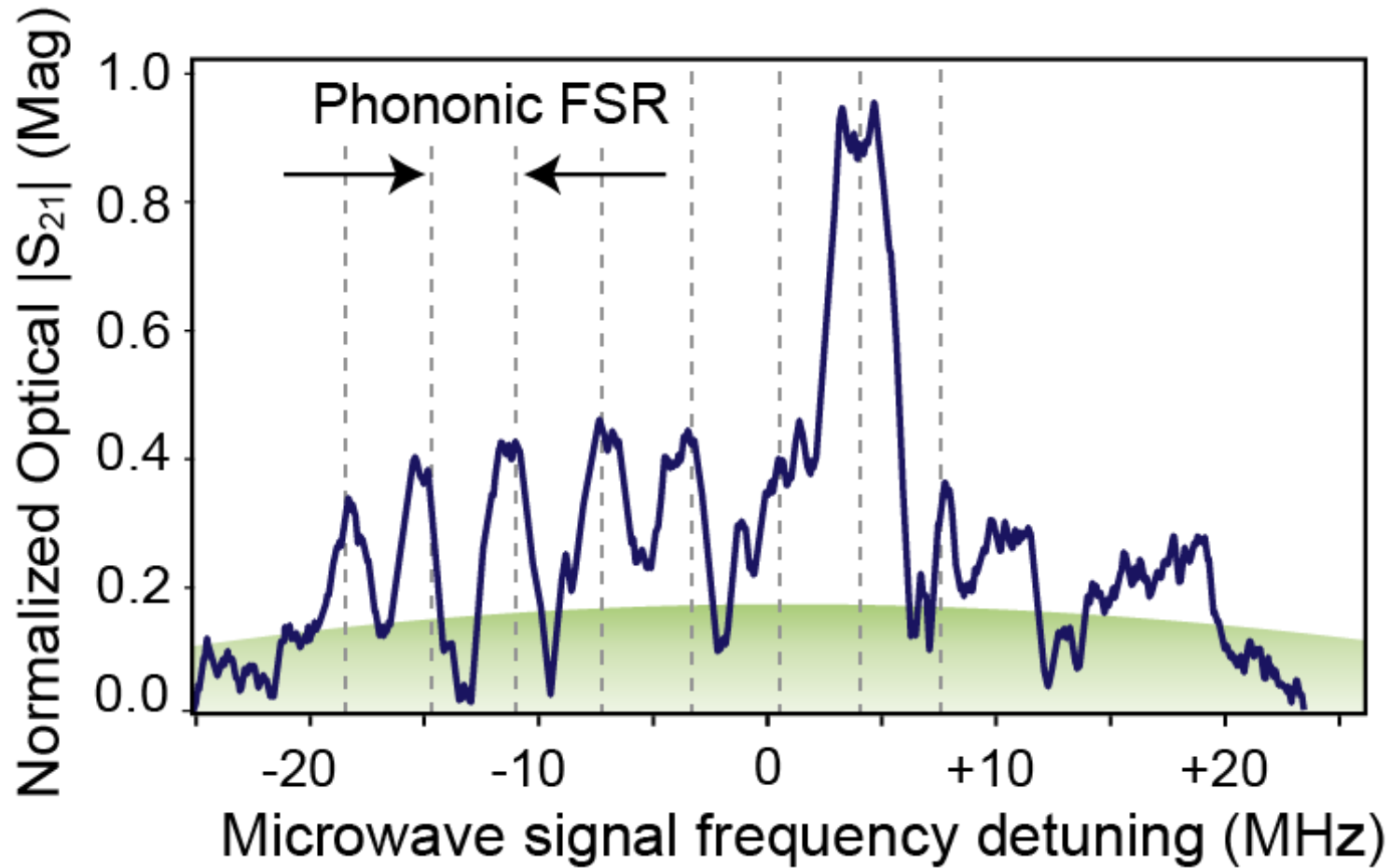
- Microwave transmission coefficient is used to measure the resonance of the phononic Love mode.
- Intrinsic quality factor $Q_L = 3K$ at 4K temperature

Multi-resonances measurement setup

Driving TE_0 resonance and a **sweeping** microwave signal



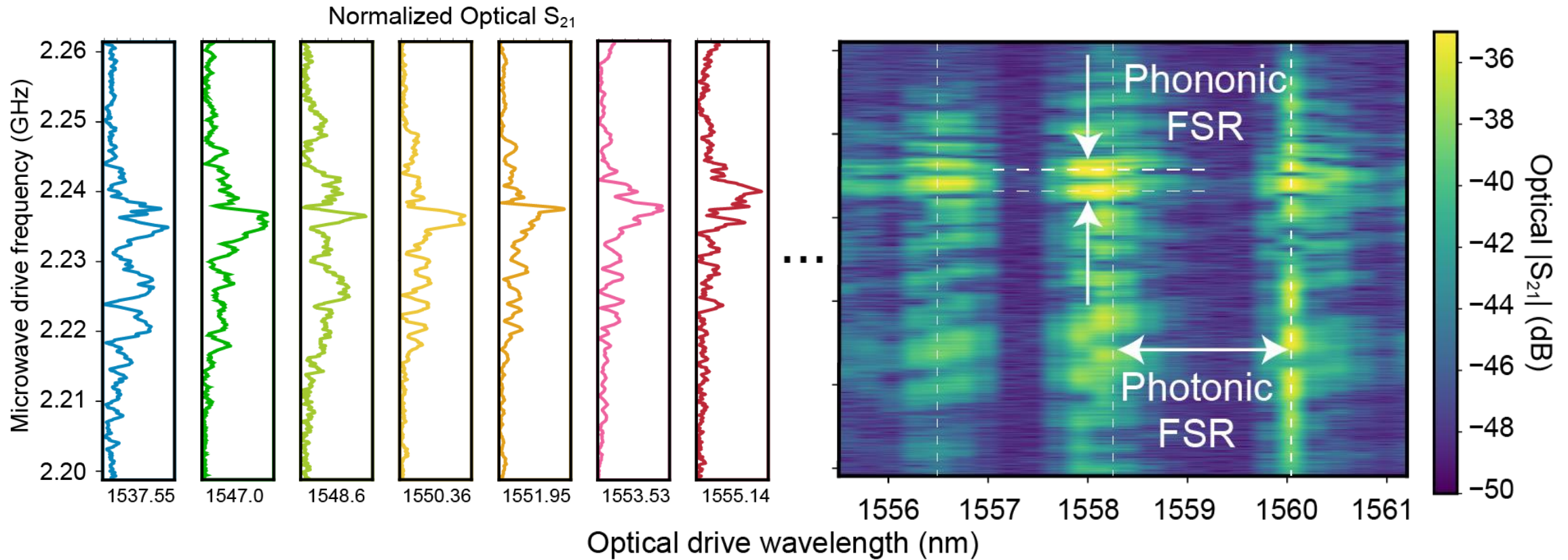
Triple resonant microwave-to-optical transduction



$$FSR = \frac{v_g}{L} \text{ (Hz)}$$

One TE_1 resonance envelopes multiple L_0 resonances, a triple resonant condition (TE_0, TE_1, L_0).

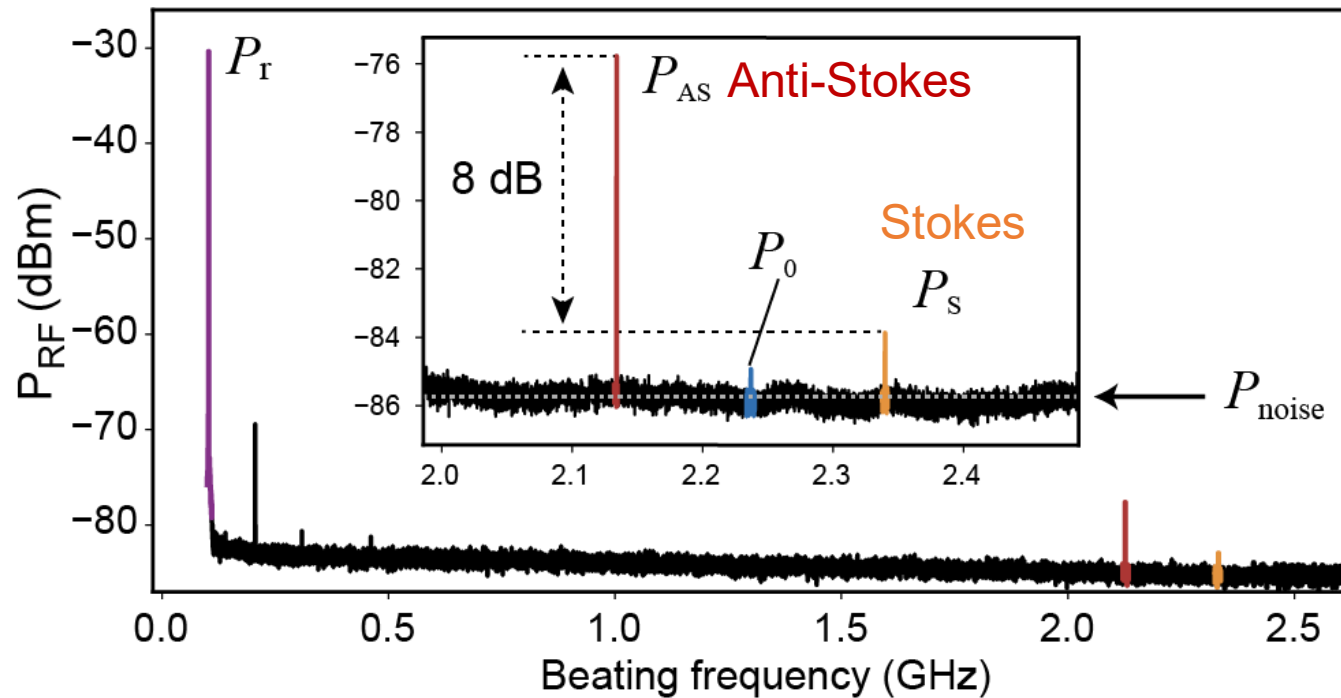
Multi-optical channels (wavelength division)



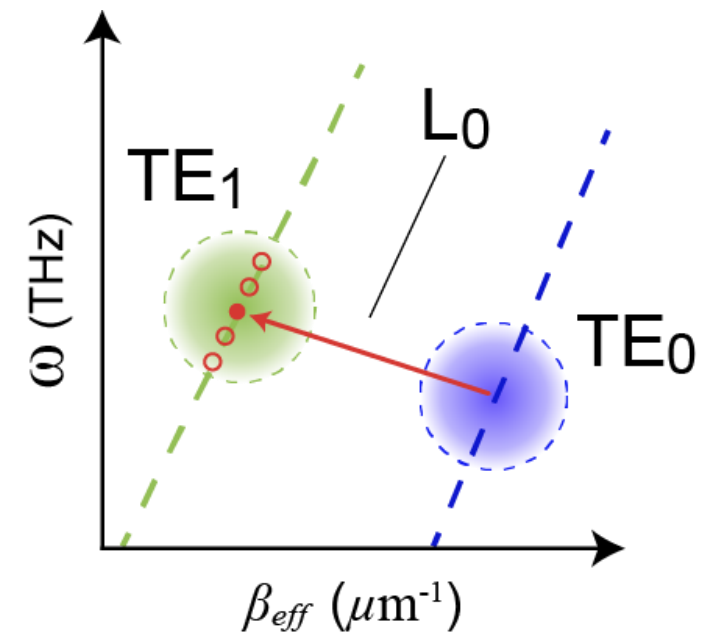
OMIC's microwave-to-optical transduction supports multiple channel/wavelengths

Heterodyne measurement

Frequency resolved anti-Stokes (phonon absorption) and Stokes (phonon emission) signal

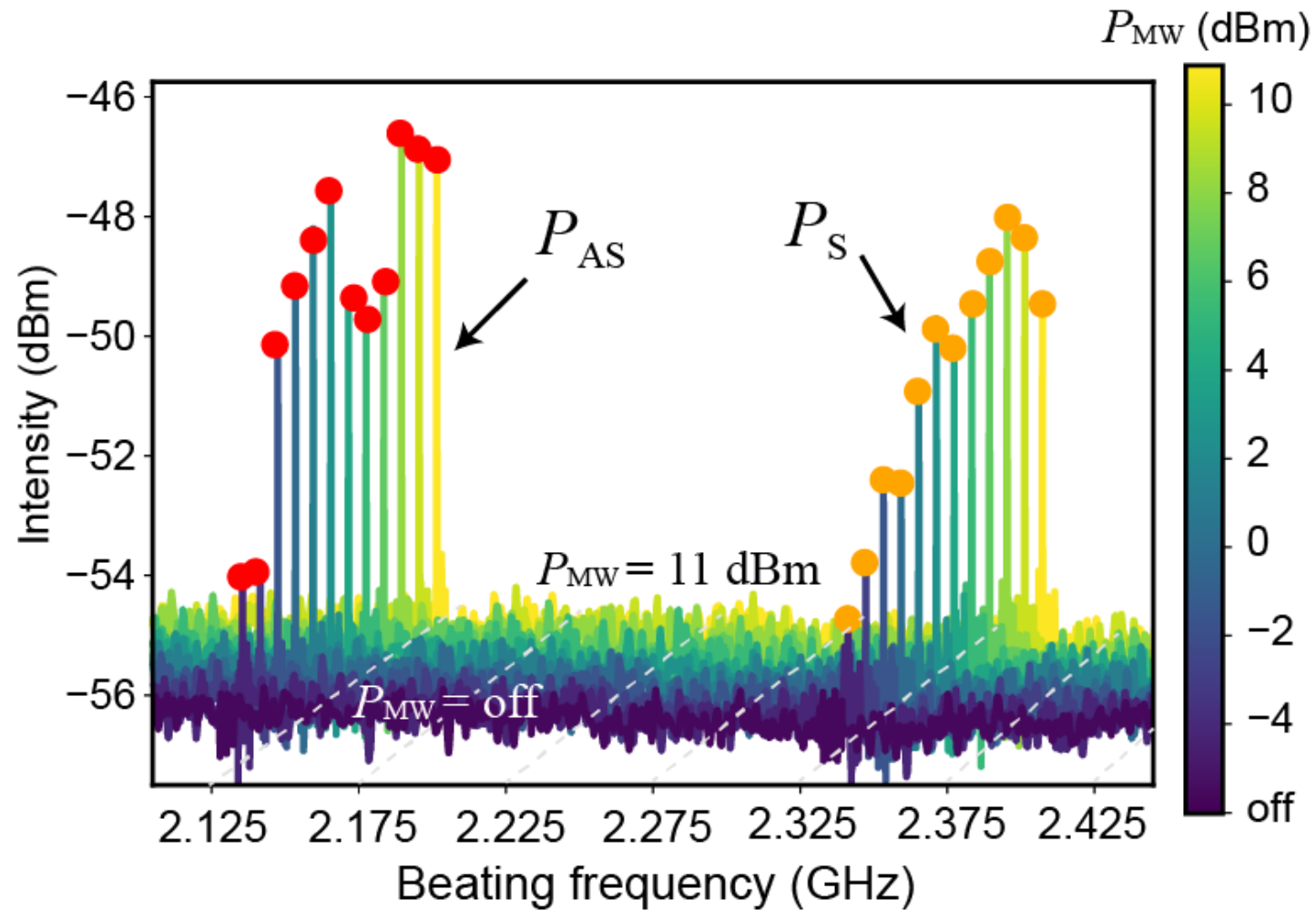


Single-frequency microwave signal



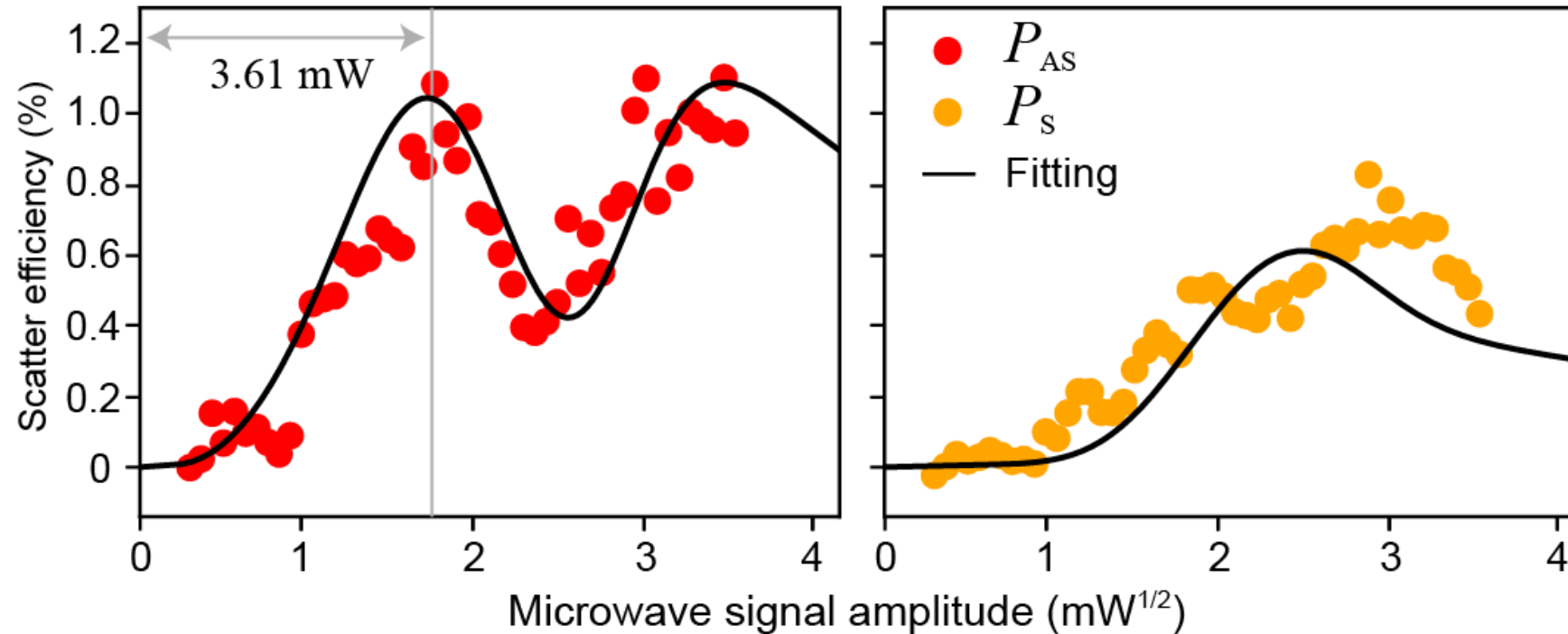
- Anti-Stokes signal dominates the intermodal microwave-to-optical conversion process
- Consistent with the phase-matching condition

Heterodyne measurements with varying microwave power



An oscillatory feature is observed when microwave power is increased

Microwave power dependent heterodyne signal



- The trace is fitted with OMIC input-output model to extract g_0
- The vacuum optomechanical coupling rate $g_0 \sim 350 \text{ Hz}$, with a theoretical limit: $g_0 = 15 \text{ kHz}$
- TE_0 -to- TE_1 efficiency saturates at 1.2%, which can be attributed to the imperfect photonic-phononic overlap

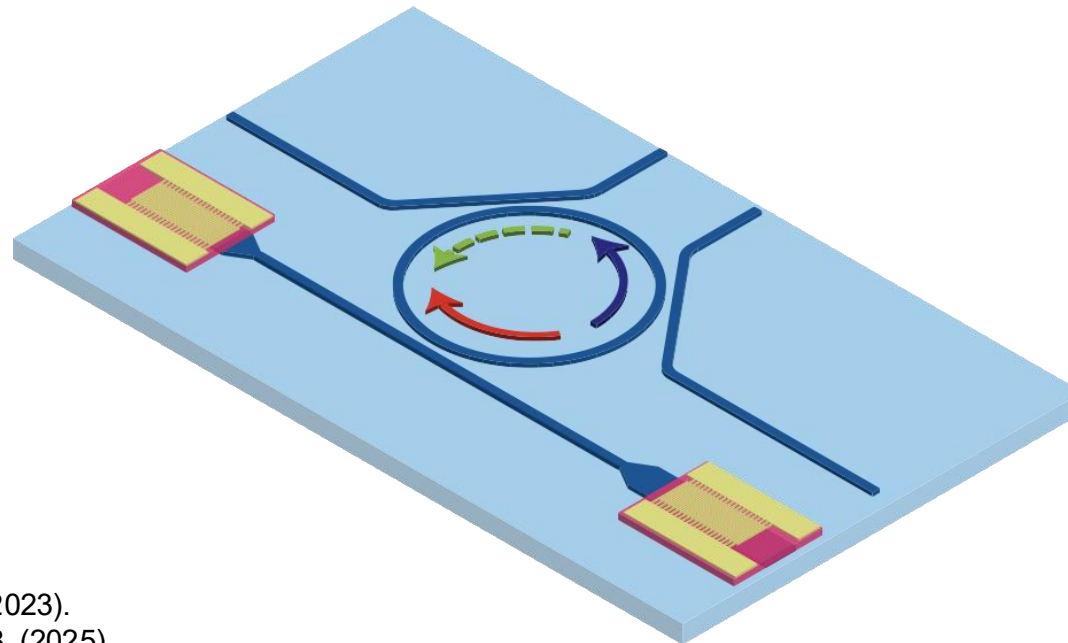
Summary and future directions

Summary

- Developed the optomechanical integrated circuit (OMIC) theory for quantum transduction
- Realized and characterized OMIC and optomechanical ring resonator (OMR)
- Utilized a scalable silicon-on-sapphire (SOS) platform for microwave-to-optical transduction

Future directions

- Works with g_0 on the same order has demonstrated qubit readout^{[1][2]}
- Quantum regime microwave-to-optical transduction
- Photon-phonon entanglement experiments
- Superconducting qubits optical read-out/control using OMIC/OMR



Transduction

$$\hat{H}_{red} = \hbar G_0 (\hat{a}_1 \hat{b}^\dagger + \hat{a}_1^\dagger \hat{b})$$

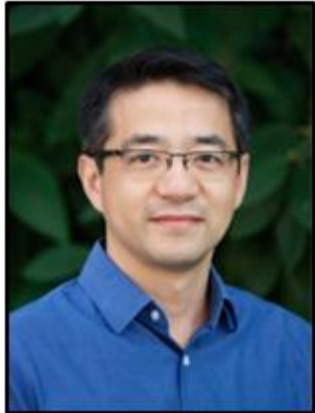
Entanglement

$$\hat{H}_{blue} = \hbar G_1 (\hat{a}_0^\dagger \hat{b}^\dagger + \hat{a}_0 \hat{b})$$

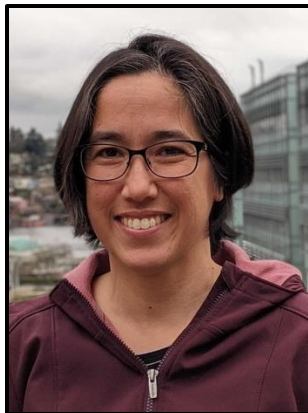
[1] Sahu, R. Science 380, 718–721 (2023).
[2] Warner, H. K., Nature Physics, 1-8. (2025)

Acknowledgements

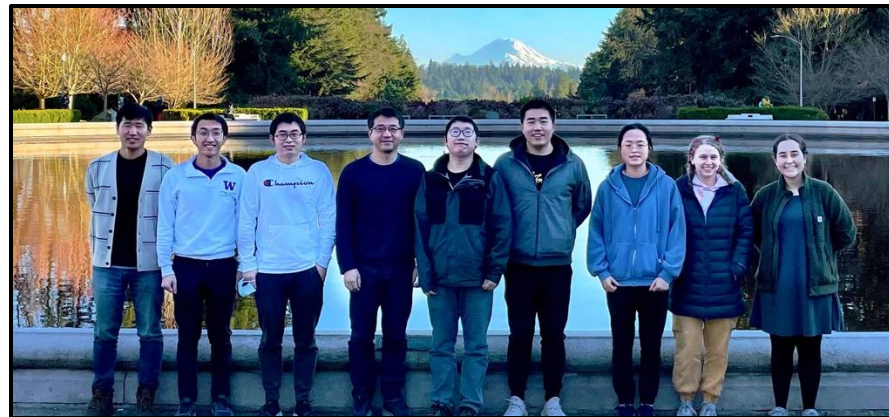
Prof. Mo Li



Prof. Kai-Mei Fu

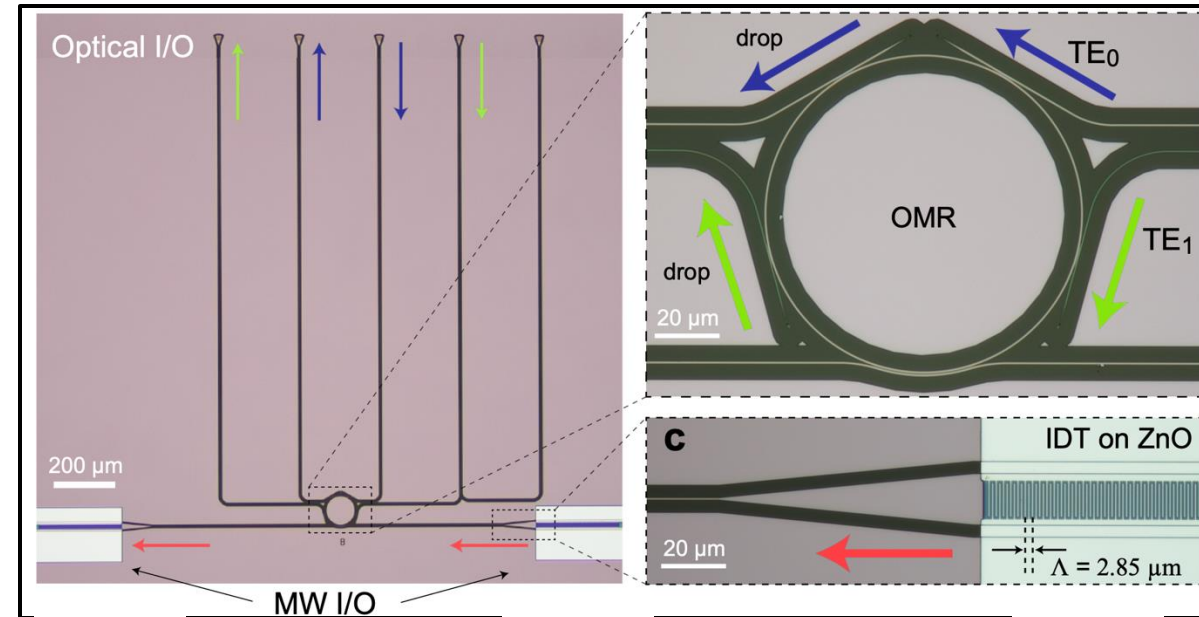
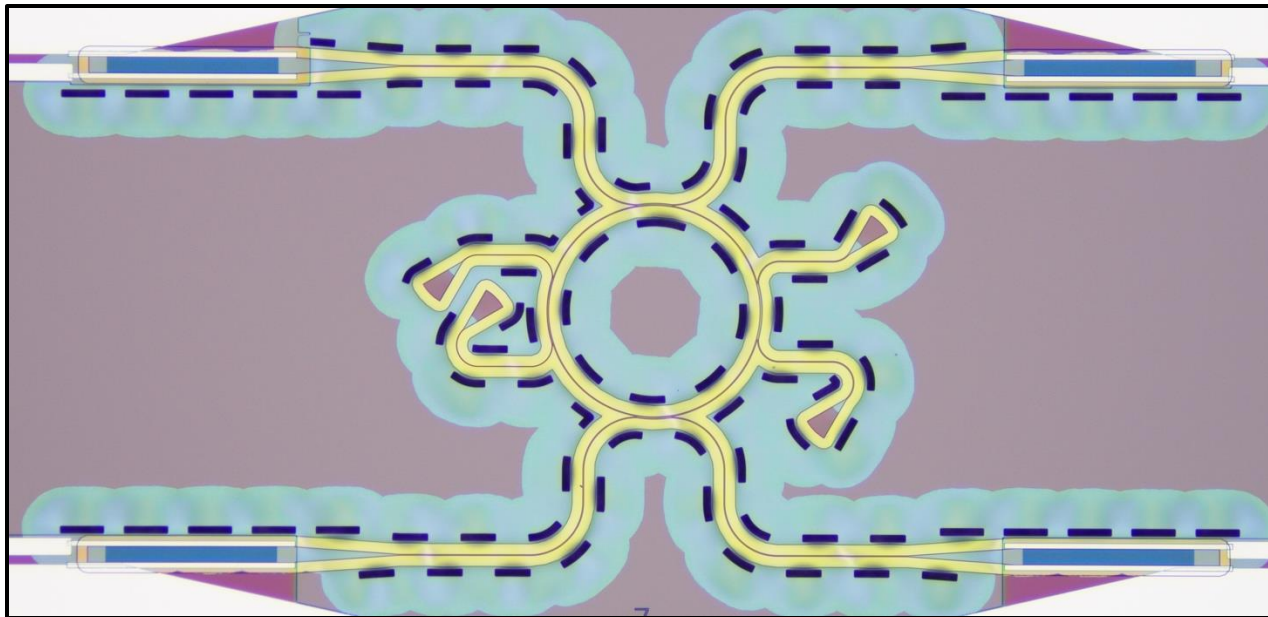


Laboratory of Photonic Systems (LPS) – Mo Li group



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Dr. Abhi Saxena
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Adina Ripin
Shucheng Fang
Ameya Velankar
Mark Han

Fundings



Supporting slides

Scalability of photonic links

Benefits of photonic links

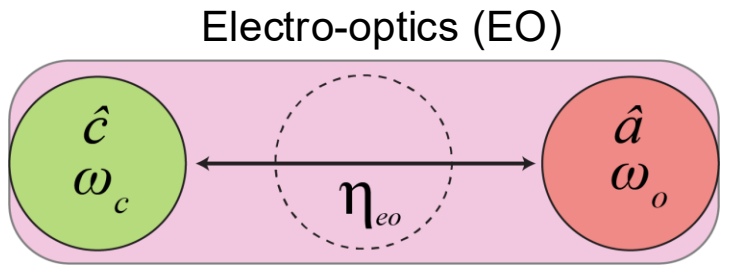
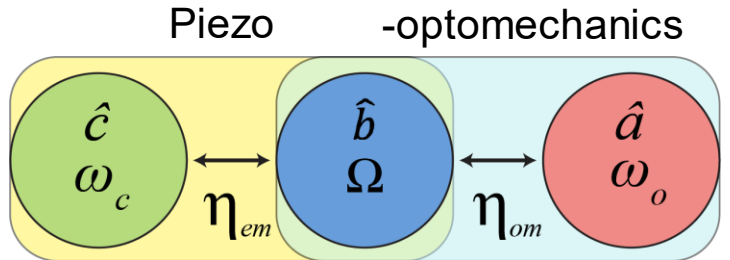
1. Low loss (temperature independent)
2. Dense wavelength division multiplexing (DWDM)
3. Reduced passive heat load at mK

Stage	Temperature	Cooling power (W)	Passive heat-load			
			Per co-axial cable	Number of cables	Per optical fiber	
4 K	$\sim 3K$	1.5	$1 \text{ mW}^{[1]}$		$5.6 \mu\text{W}^{[2]}$	Number of fibers 10^6
MXC	$\sim 0.006K$	19×10^{-6}	$\sim 10 \text{ nW}^{[3]}$	10^3	$\sim 5 \text{ pW}^{[3]}$	

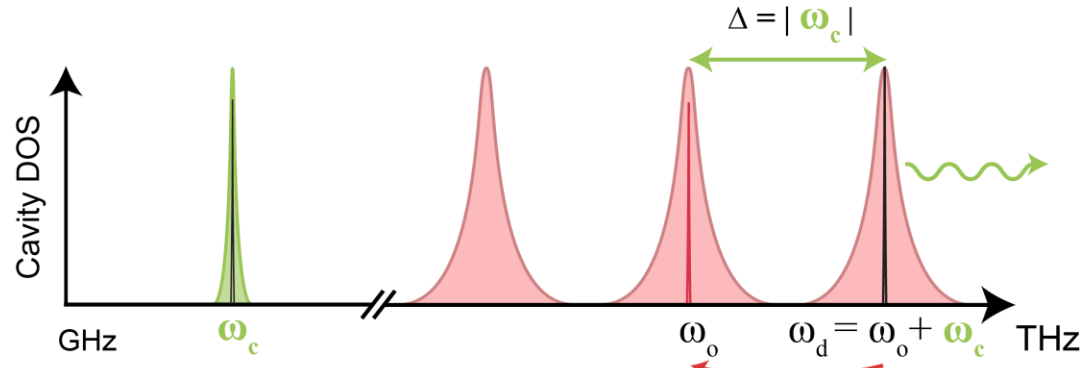
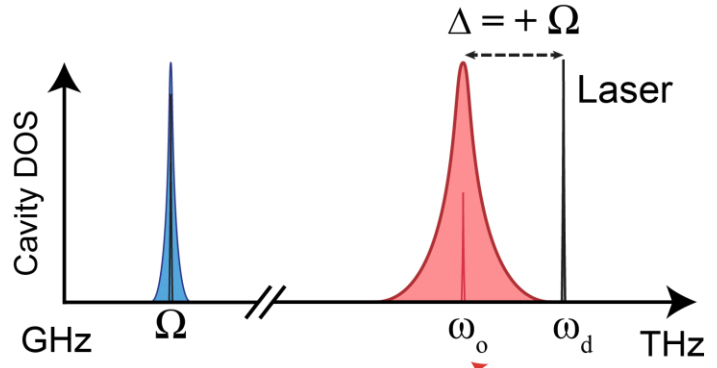
Multi-channel photonic link at telecommunication band (1310nm or 1550nm) *for each fiber*

This requires microwave-to-optical transduction!

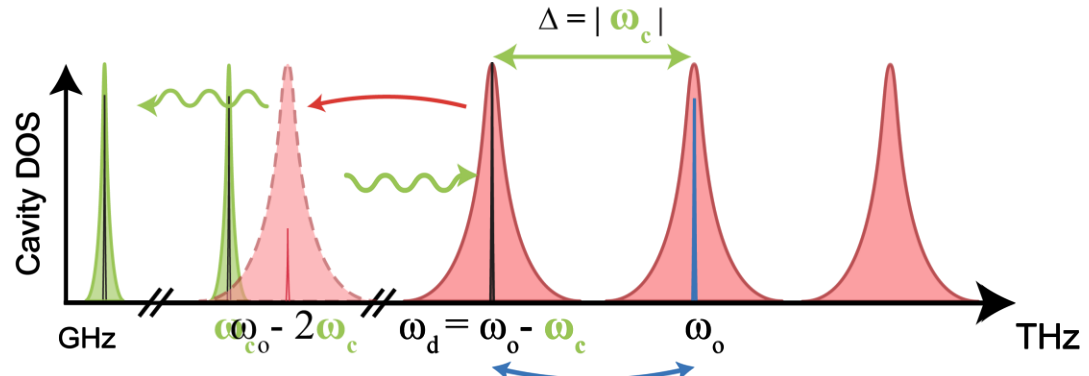
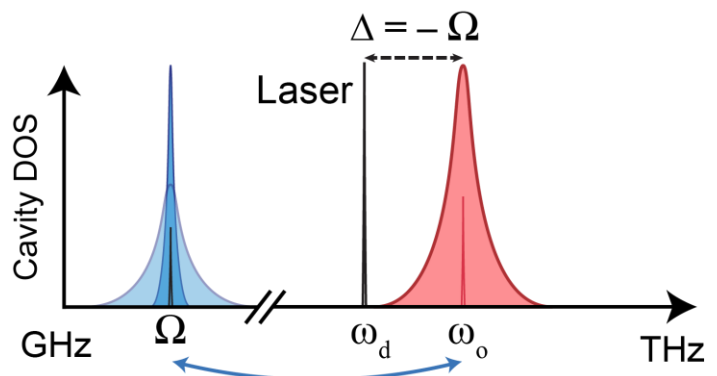
[1] Krinner et al., *EPJ Quantum Technology*, 6(1), p.2. (2019)
[2] S. Joshi and S. Moazeni, *Journal of Lightwave Technology*, (2024)
[3] Lecocq, F., et al. *Nature* **591**, 575–579 (2021).



$$\hat{H}_{blue} = \hbar g(\delta \hat{a} \hat{b} + \delta \hat{a}^\dagger \hat{b}^\dagger)$$



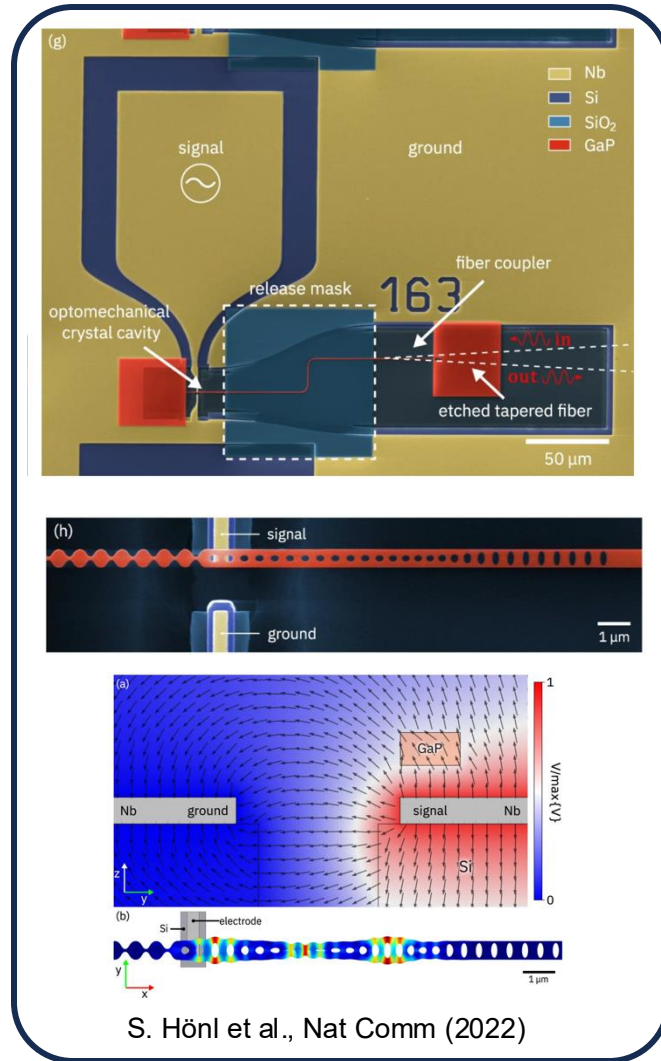
$$\hat{H}_{red} = \hbar g(\delta \hat{a} \hat{b}^\dagger + \delta \hat{a}^\dagger \hat{b})$$



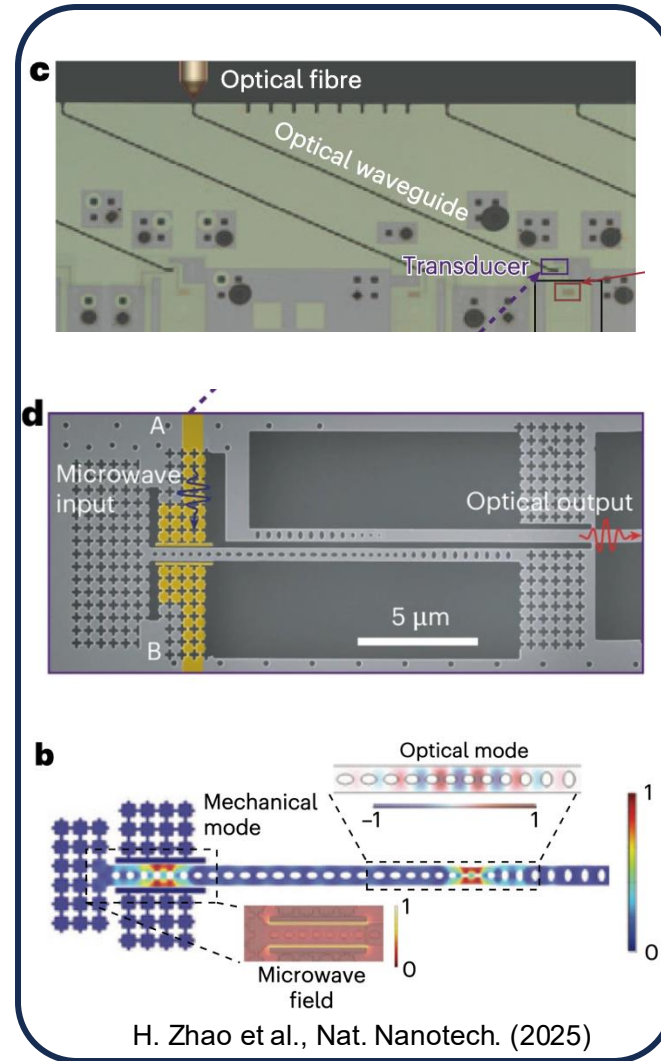
Parasitic down-conversion

Different material systems for microwave-optical transduction

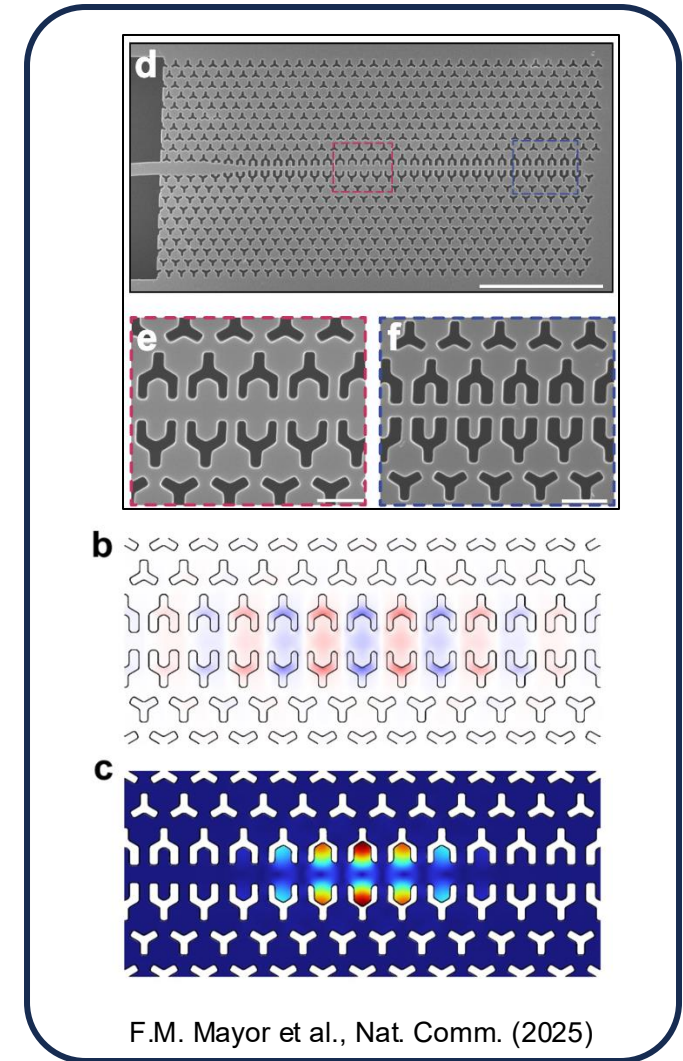
Gallium phosphide (GaP) 1D OMC



NbTiN on silicon (no piezo)



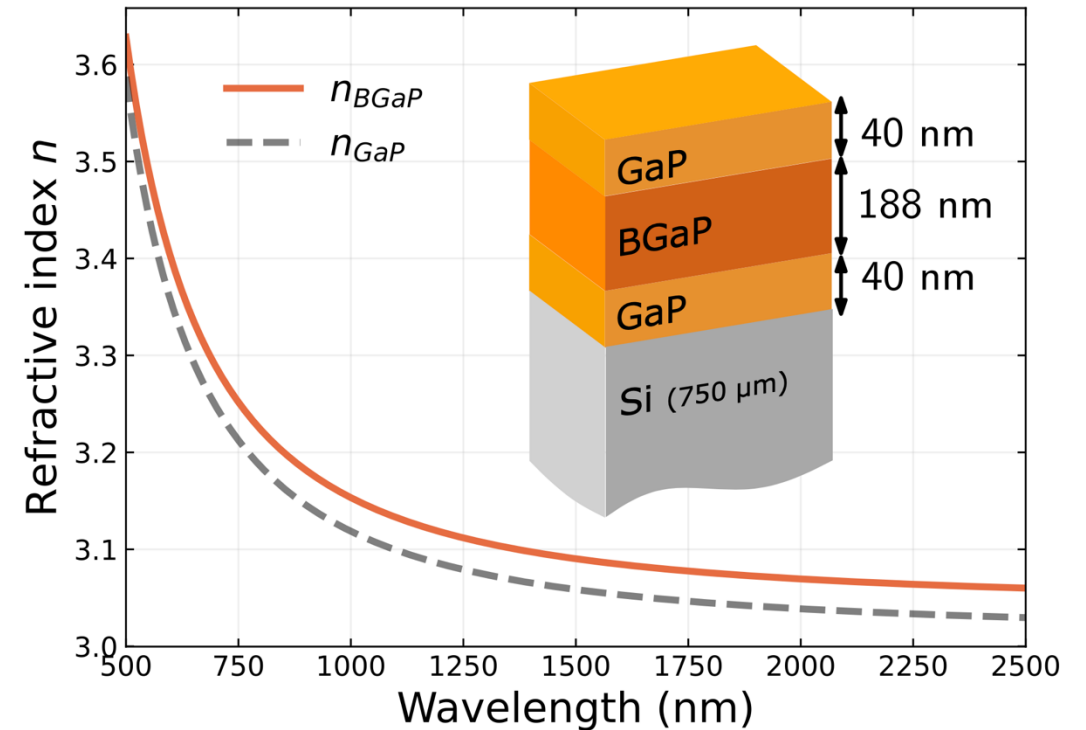
silicon (no piezo) 2D OMC



How to improve device scalability for integration?

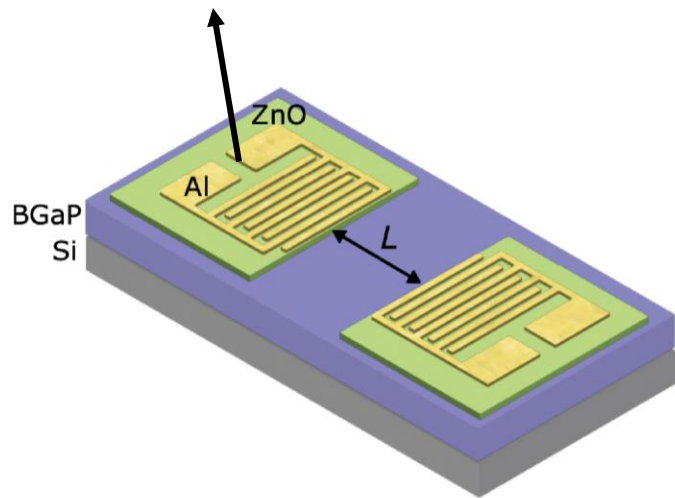
Boron-doped Gallium Phosphide (BGaP)

- High refractive index $n \sim 3.1$ (1550 nm)
- High acousto-optic figure or merit $\mathcal{M}^{(2)}$, $\sim n^6$
- Slow acoustic speed $v \sim 4000$ m/s
- Large second-order nonlinearity $\chi^{(2)} \sim 110$ pm/V
- Low piezoelectricity



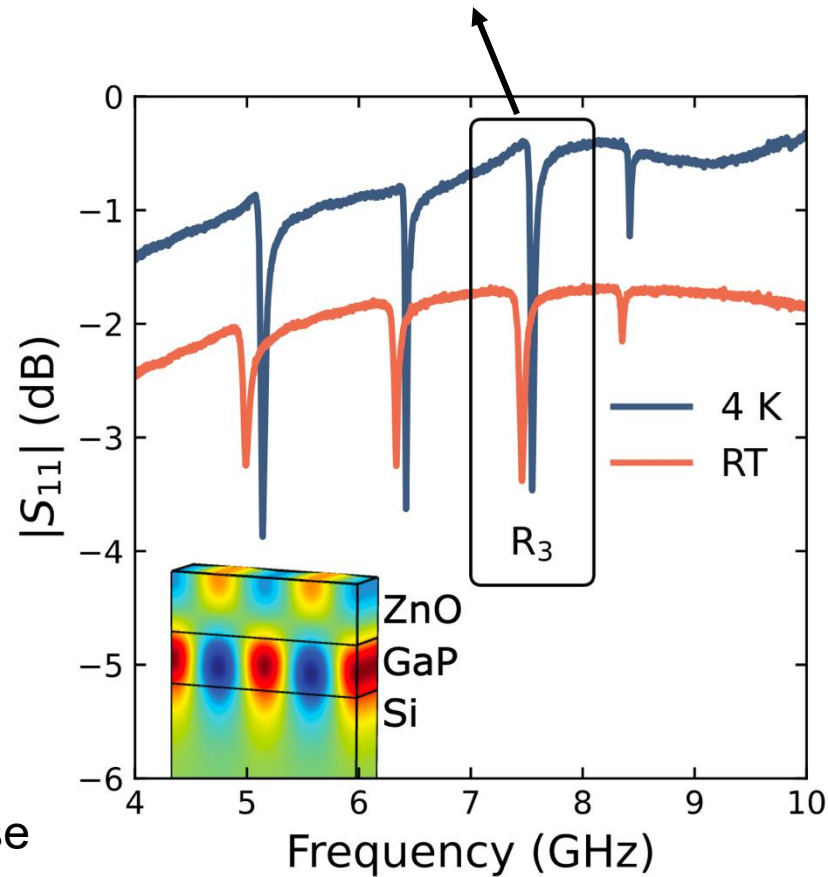
Boron-doped Gallium Phosphide (BGaP): Acoustic Characterizations

Interdigital transducer (IDT) on zinc oxide (ZnO)

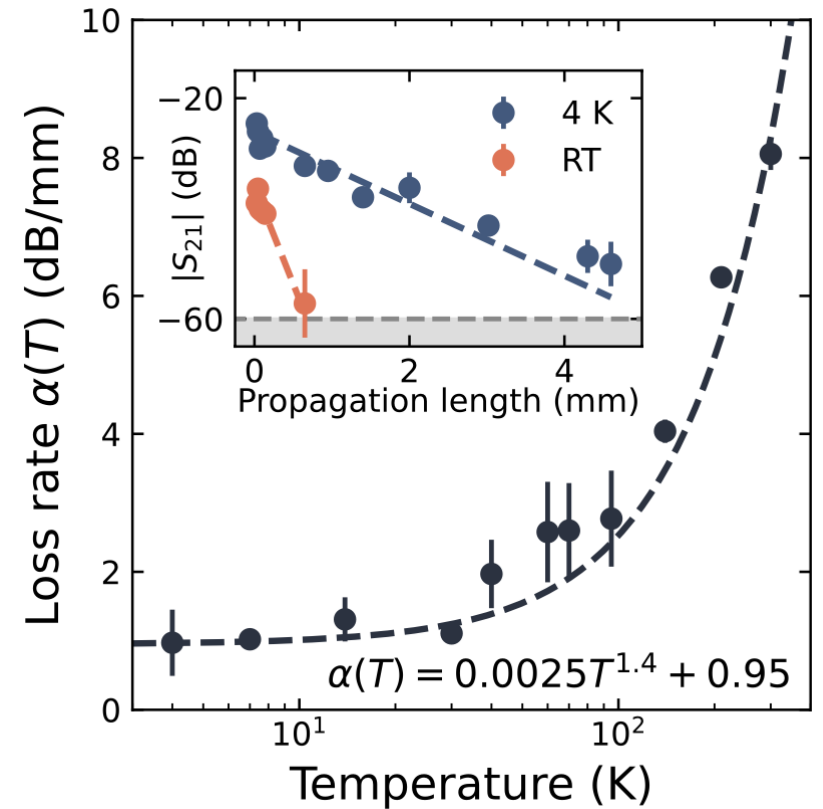


ZnO:
Strongly piezoelectric
Thin-film can be sputtered in house
Easy to integrate

High-order phononic mode

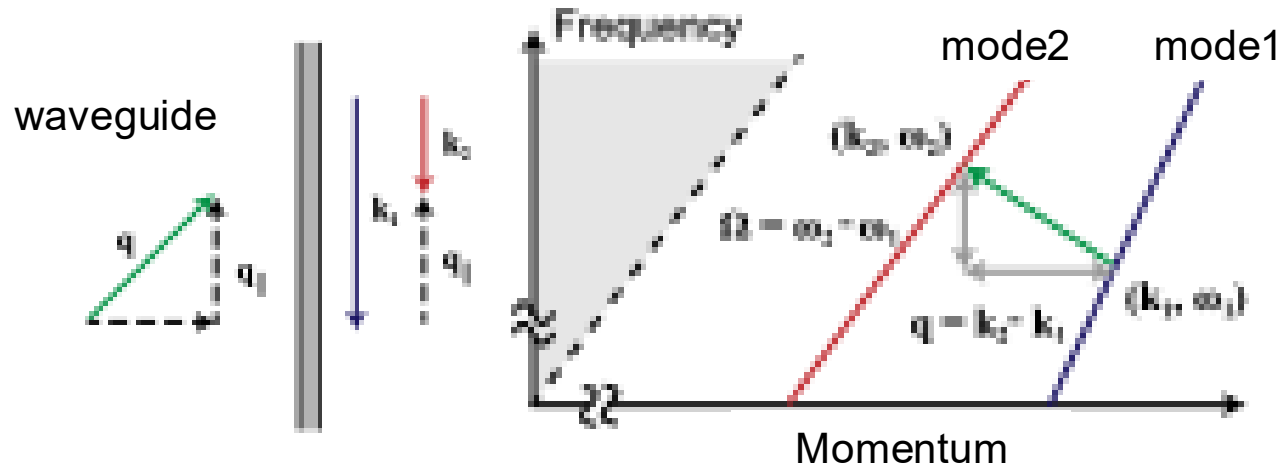


< 1dB/mm propagation loss at 4K



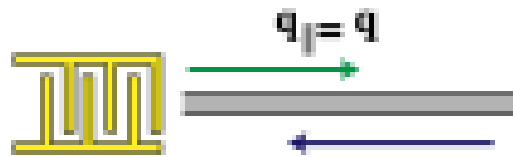
Intermodal Brillouin Scattering

Microwave-to-optical transduction through intermodal Brillouin scattering



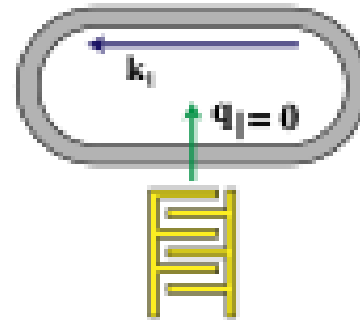
Type I: $q_{\parallel} = k$

Q. Liu, H. Li, and M. Li, Optica (2019)



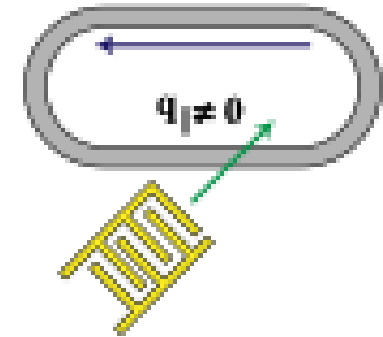
Type II: $q_{\parallel} = 0$

S. A. Tadesse and M. Li, Nat. Comm. (2014)



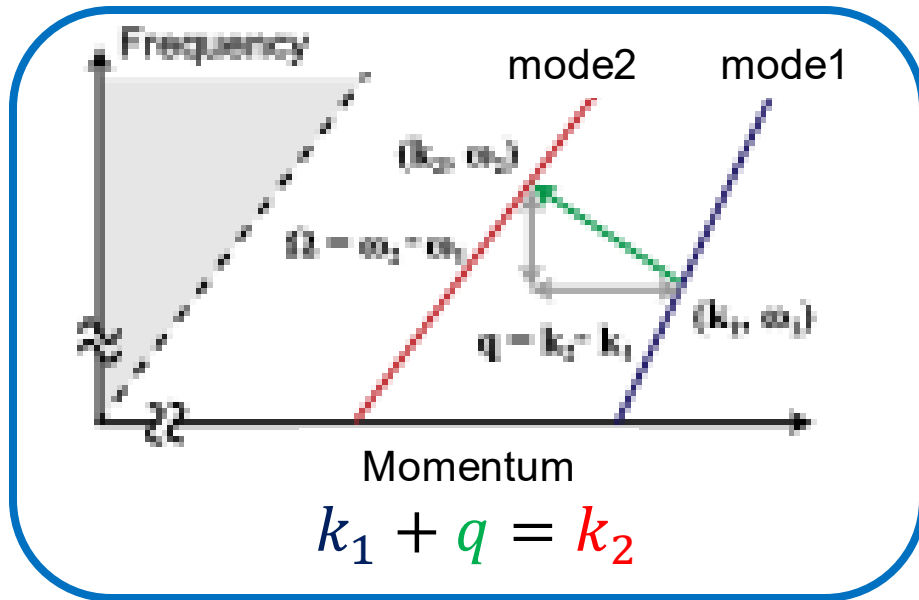
Type III: $q_{\parallel} \neq 0$

D. B. Sohn et al., Nat. Photonics (2018)



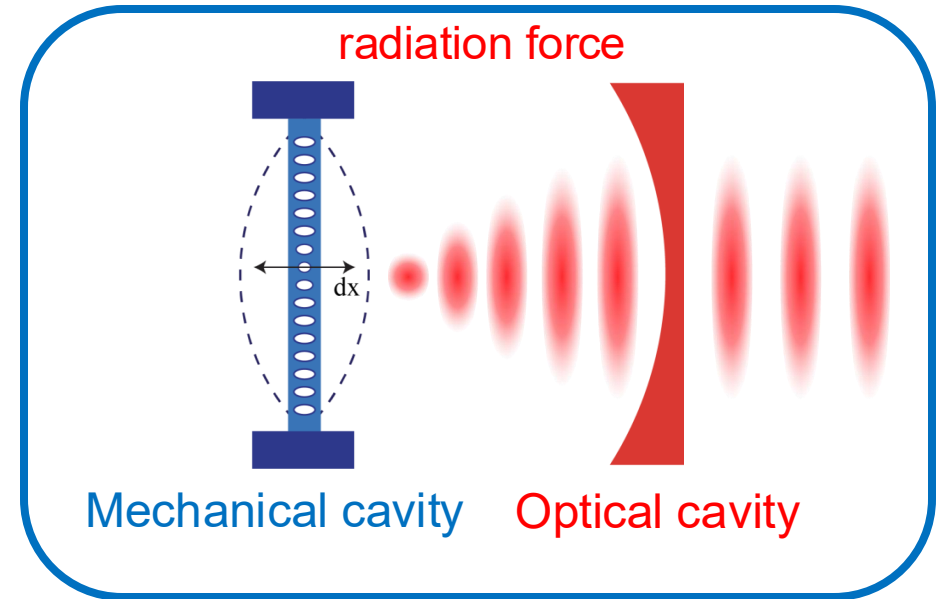
These do not utilize resonating phononic modes

Intermodal Brillouin scattering in waveguides



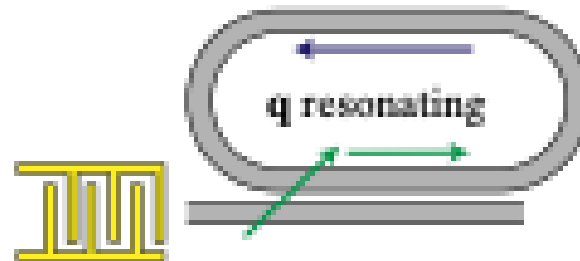
+

Cavity-optomechanics



Type IV: Co-resonant phononic mode

Optomechanical integrated circuit (OMIC)



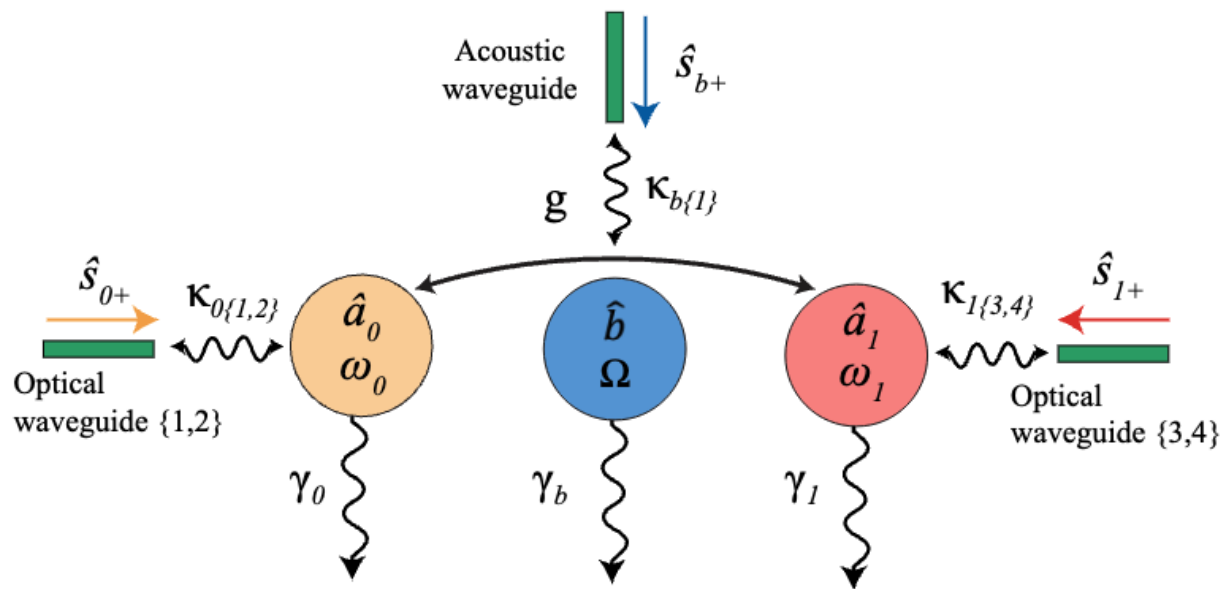


FIG. S1. Overview diagram of the system model.

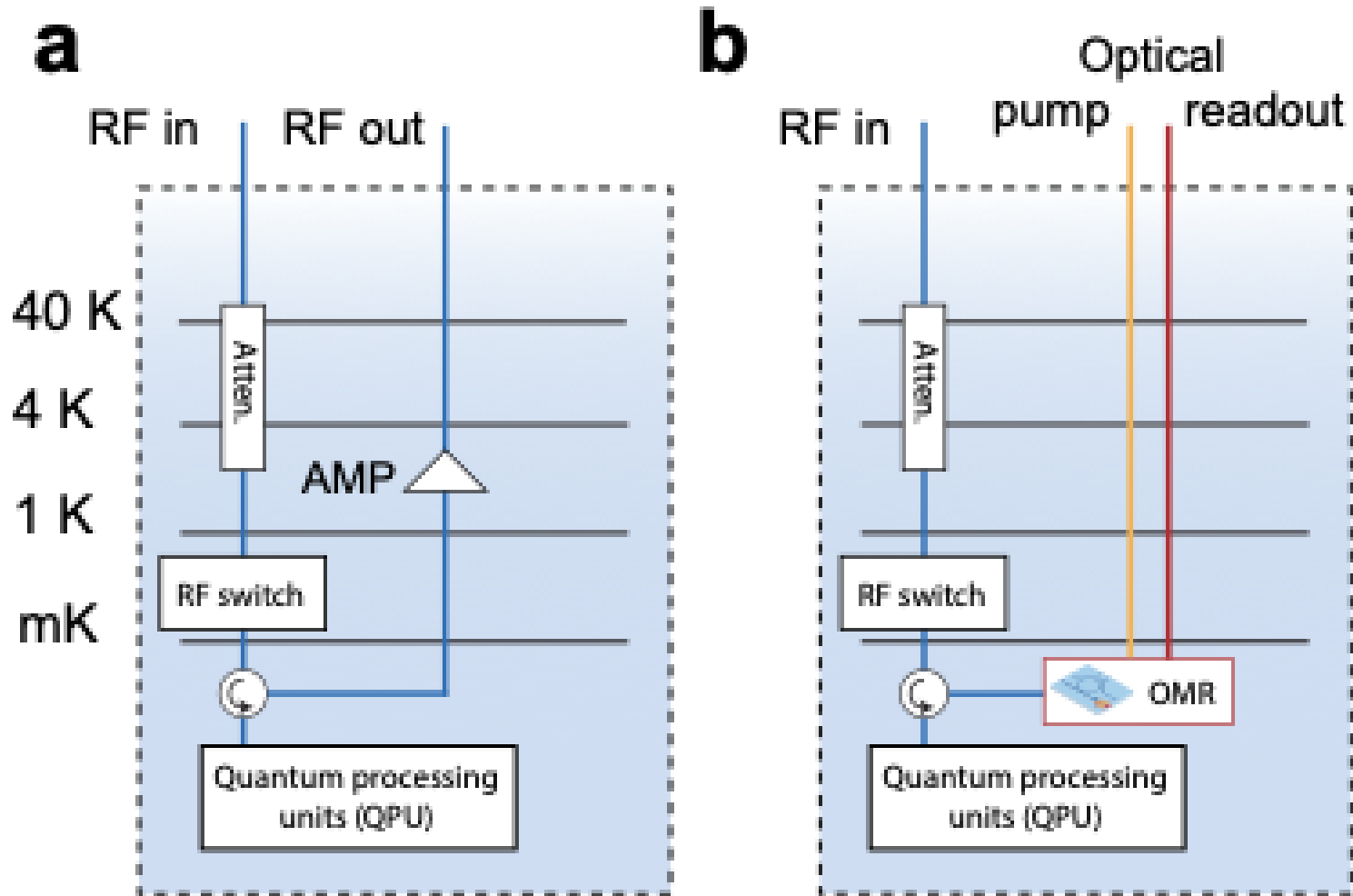
EOM

$$\begin{aligned}\dot{\hat{a}}_0 &= -i\omega_0\hat{a}_0 - ig_0\hat{a}_1\hat{b}^\dagger - \left(\hat{s}_{0+}\sqrt{\gamma_0} + \frac{\sqrt{\kappa_{0,1}\kappa_{0,2}}}{2}\hat{a}_0 + \frac{\sqrt{\kappa_{0,1}\kappa_{1,3}}}{2}\hat{a}_1 \right), \\ \dot{\hat{a}}_1 &= -i\omega_1\hat{a}_1 - ig_0\hat{a}_0\hat{b} - \left(\hat{s}_{1+}\sqrt{\gamma_1} + \frac{\sqrt{\kappa_{1,3}\kappa_{0,1}}}{2}\hat{a}_0 + \frac{\sqrt{\kappa_{1,3}\kappa_{1,4}}}{2}\hat{a}_1 \right), \\ \dot{\hat{b}} &= -i\Omega_0\hat{b} - ig_0\hat{a}_0^\dagger\hat{a}_1 - \left(\hat{s}_{b+}\sqrt{\gamma_b} + \frac{\gamma_b}{2}\hat{b} \right),\end{aligned}$$

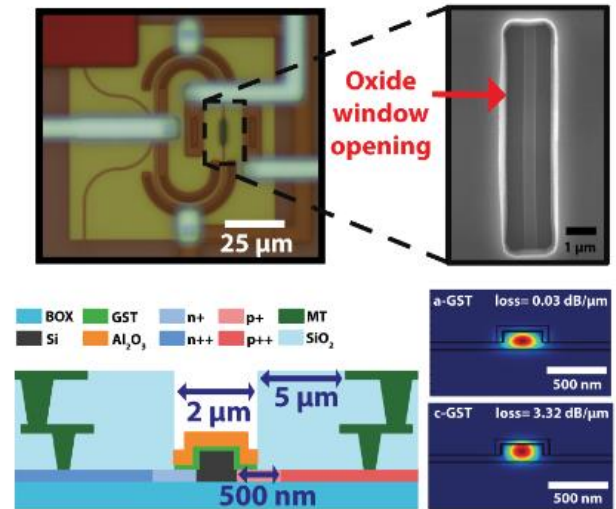
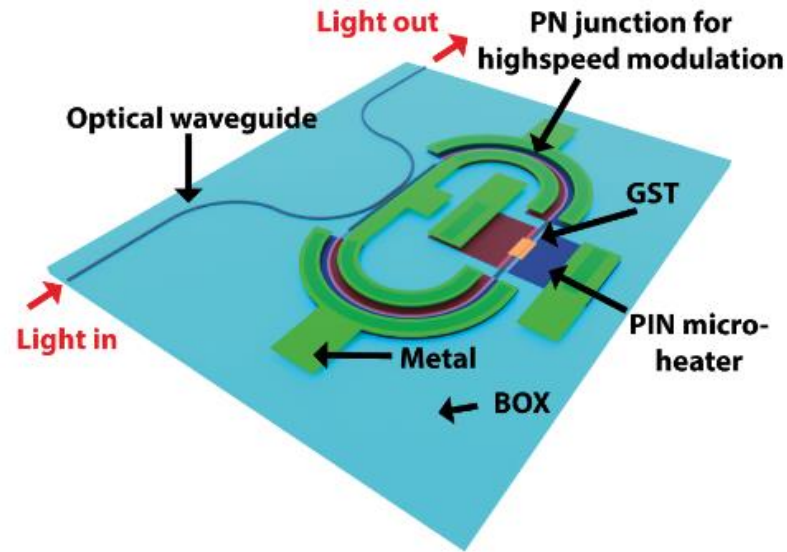
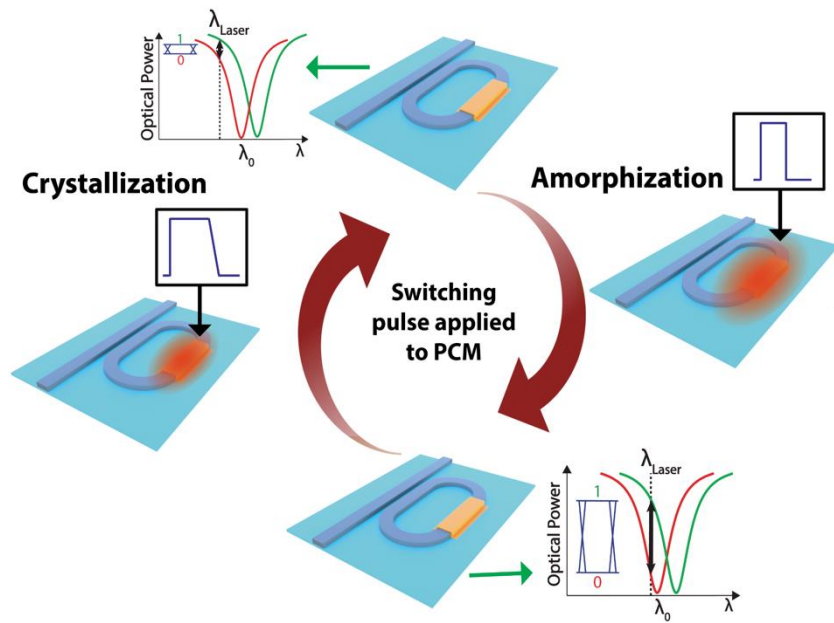
input-output theory

$$\begin{aligned}\hat{s}_{0,r-} &= \hat{s}_{r+} + \sqrt{\gamma_{0,r}}\hat{a}_0, \\ \hat{s}_{1,r-} &= \hat{s}_{r+} + \sqrt{\gamma_{1,r}}\hat{a}_1, \\ \hat{s}_{b,-} &= \hat{s}_{+} + \sqrt{\gamma_b}\hat{b}.\end{aligned}$$

Summary and future directions



Non-volatile Tuning of Cryogenic Optical Resonators at 4K



- Non-volatile phase-changing material (PCM)
- Set-and-forget. No DC bias required
- Commercial process taped out to AMF
- Post-process PCM-GST deposition in-house

